# Inelastic Demand Meets Optimal Supply of Risky Sovereign Bonds\*

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#### Abstract

We present evidence of inelastic demand in the market for risky sovereign bonds and examine how it affects government policies. We exploit monthly changes in the composition of a major emerging market bond index to identify flow shocks that shift the available bond supply, which are unrelated to country fundamentals. Our estimates imply an average inverse price demand elasticity of -0.30, higher in magnitude than estimates for advanced economies. This elasticity increases with default risk, suggesting that investors demand a premium as compensation for risk. We develop a sovereign debt model with endogenous default, and we discipline it based on our empirical estimates. Under inelastic investors, an additional unit of debt lowers bond prices even under constant default risk. Because governments internalize this effect, the inelastic demand becomes a commitment device that limits debt issuances. Our quantitative model shows that this mechanism significantly reduces default risk and bond spreads.

**Keywords:** emerging markets bond index, inelastic financial markets, institutional investors, international capital markets, small open economies, sovereign debt

**JEL Codes:** F34, F41, G11, G15

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## 1 Introduction

Governments in emerging economies heavily depend on bonds issued in liquid international capital markets for their overall financing. The behavior of investors in these markets is thus crucial to understanding governments' borrowing costs, default risk, and optimal debt management. Standard sovereign debt models often assume that investor demand is perfectly elastic, implying that investors are willing to lend any amount governments request at the risk-free rate plus a default risk premium. This assumption on investor behavior contrasts with a body of recent work for other asset markets that allows for a richer demand structure, typically involving an inelastic or downward-sloping demand (Koijen and Yogo, 2019; Gabaix and Koijen, 2021; Vayanos and Vila, 2021; Gourinchas et al., 2022; Greenwood et al., 2023).

In this paper, we present novel evidence of downward-sloping demand curves in risky sovereign bond markets and analyze their impact on governments' optimal debt policies. We first estimate high-frequency bond price reactions to flow shocks unrelated to fundamentals, using monthly variation in the composition of the largest benchmark index for dollar-denominated bonds from emerging economies. Changes in this index affect the demand of passive investors that seek to replicate its composition and imply a shift in the supply of bonds available to active investors. We find that bond prices significantly react to these shocks, even though they are orthogonal to country fundamentals. Our estimates imply an inverse price demand elasticity of -0.30, which we refer to as a reduced-form elasticity.

We then formulate a quantitative sovereign debt model that features endogenous bond issuances and default risk, and discipline it based on our reduced-form estimates. The goal of the model is twofold. First, we use the model to isolate the part of the estimated reduced-form elasticity that is explained by endogenous responses in government debt policy and bonds' future payoffs so as to identify a structural elasticity. Our findings show that over one-third of the reduced-form elasticity is explained by these endogenous forces. Second, we analyze the aggregate implications of a downward-sloping demand in risky sovereign debt markets. We show that, in the presence of inelastic investors, an additional unit of debt leads to a decrease in bond prices even if default risk is constant, thereby increasing the government's borrowing costs. Since governments internalize this effect, an inelastic demand limits debt issuances and acts as a commitment device. Using our calibrated model, we show that this channel significantly reduces default risk and bond spreads.

We start our analysis with a simple framework to guide our empirical analysis. This setup features investors who are heterogeneous in their degree of activism (or passivism), i.e.,

in how they allocate their funds across risky assets. We define the passive demand as the portion of investors' holdings aimed at replicating the composition of the index they follow. Passive demand is perfectly inelastic and only shifts with changes in index weights. For any asset in fixed supply, a higher passive demand implies a leftward shift in the "effective supply," which refers to the quantity of bonds available to active investors. If this shift is unrelated to country fundamentals, and assuming that future asset payoffs remain fixed, this variation can be used to examine whether active investors' demand curves slope downward and to measure their demand elasticity (Pandolfi and Williams, 2019; Pavlova and Sikorskaya, 2022). Nevertheless, if expected payoffs endogenously respond to changes in the effective supply, any observed price variation resulting from the shift could over or underestimate the demand elasticity. Since asset prices and payoffs are jointly determined, this potential response motivates the need of a structural model in which prices, the bond supply, and expected payoffs are endogenous outcomes.

On the empirical front, we identify exogenous shifts in a country's effective supply of sovereign bonds by exploiting monthly rebalancings in the J.P. Morgan Emerging Markets Bond Index Global Diversified (EMBIGD). This index covers U.S. dollar-denominated sovereign bonds issued by emerging economies and is the most widely used as benchmark by institutional investors operating in those markets. Changes in the composition of this index affect the effective bond supply available to active investors, as they trigger similar rebalancings in the portfolios of passive investors who aim to replicate the index to minimize potential tracking error costs. Given the EMBIGD's prominence, these rebalancings can have market-wide effects and affect sovereign bond prices.

Rebalancings in the EMBIGD take place on the last trading day of each month and are essentially driven by the inclusion of new qualifying bonds into the index or the removal of maturing ones. The substantial number of investors tracking the EMBIGD means that these changes in country weights trigger large passive fund flows. By combining monthly changes in index weights with the assets passively tracking the index, we construct, for each country in each month, a measure of flows implied by the rebalancing (FIR), which we use to estimate a reduced-form demand elasticity in this market. To avoid endogeneity issues, we construct an instrument that exploits changes in the FIR that arise solely due to the issuance or retirement of bonds from other countries in the index, which are unrelated to changes in bond prices of the country in question from one month to another. As such, these changes are orthogonal to a country's own fundamentals. By combining this instrument with the specific timing of the reabalancing, we can estimate how bond prices react to passive demand

shocks within a small time window around each rebalancing date.

Our analysis reveals that a higher FIR leads to higher bond prices. On average, a 1 percentage point (p.p.) increase in the FIR corresponds to a 30 basis point increase in bond prices. These estimates imply a reduced-form inverse demand elasticity of -0.30. We find that these price reactions vary across countries with different levels of default risk. Specifically, for countries with higher default risk, a 1 p.p. FIR inflow can result in up to a 41 basis point increase in bond prices. In contrast, for safer countries, the estimates are smaller (an 11 basis point increase) and statistically not significant. Overall, these findings suggest that investors demand a premium as compensation for holding risky bonds, which gives rise to an inconvenience yield.

On the quantitative front, we formulate a sovereign debt model where the government has limited commitment and can endogenously default on its debt obligations. Standard models of this nature typically assume a perfectly elastic demand for sovereign bonds, with changes in bond prices driven solely by variations in default risk (Arellano, 2008; Chatterjee and Eyigungor, 2012). We extend these models using a richer demand structure that includes both active and passive investors and a downward-sloping demand curve for active investors that is modeled following Gabaix and Koijen (2021). Specifically, we assume that active investors have a mandate that specifies how they should allocate their funds. They can deviate from that mandate based on bonds' expected returns but are limited in the extent to which they can do so. To create a tight link with our empirical analysis, we introduce secondary markets where bonds are traded. In this way, by shocking the passive demand, we can replicate within the model our empirical reduced-form elasticity.

We use the calibrated model to decompose the estimated reduced-form elasticity into two components: the actual slope of the active investors' demand curve, i.e., the structural elasticity, and the part of the price reaction that captures changes in future bond issuances and expected payoffs. We find that these endogenous responses account for a third of the reduced-form elasticity, and that the effects are larger the higher the persistence of the shock. Overall, our results underscore the importance of accounting for issuers' endogenous responses and changes in the expected repayment of assets. These factors must be considered to avoid potential biases in estimating demand elasticities. Our FIR measure is inherently more temporary than other instruments used in the literature, such as index additions or deletions or index methodological recompositions. Still, we find that the endogenous changes in expected bond repayments can account for about one-third of the total price response.

More importantly, our model allows us to examine the impact of a downward-sloping

demand on the optimal debt and default policies of governments. In the presence of an inelastic demand, we observe lower default risk and higher bond prices compared to a scenario with a perfectly elastic demand and similar debt levels. This outcome is not driven by a convenience yield (i.e., a higher price that investors are willing to pay for the bond) but rather by the inelastic demand serving as a commitment device for the government. The mechanism behind it is as follows: with a downward-sloping demand, issuing an additional unit of debt decreases bond prices even if default risk remains fixed. As a result, the government finds issuing large amounts of debt too costly and opts not to do so. An inelastic demand thus limits the maximum amount of debt the government is willing to issue. In our quantitative analysis, we find that this limit leads to a large reduction in default risk and bond spreads. Apart from the commitment device, an inelastic demand imposes some costs because it leads to a debt policy that is less responsive to shocks. Overall, we find that the benefits derived from the commitment device dominate and the government is better off in the presence of inelastic investors.

Our findings contribute to various strands of literature. First, we contribute to a long-standing literature using index rebalancings to estimate asset price reactions, demand elasticities, and changes in investors' portfolios across different asset classes (Harris and Gurel, 1986; Shleifer, 1986; Greenwood, 2005; Hau et al., 2010; Chang et al., 2014; Raddatz et al., 2017; Pandolfi and Williams, 2019; Pavlova and Sikorskaya, 2022). Our contribution lies in showing that demand curves slope downward in one of the most relevant markets for government financing in emerging economies: the international U.S. dollar bond market.

An important contribution of our work is showing that, even in response to exogenous supply-shifting shocks, part of the price movement can be attributed to changes in assets' expected payoffs, rather than solely reflecting an inelastic demand component. Our analysis can be applied to any asset, beyond sovereign bonds, whose future cash flows or payoffs are affected by movements in the effective supply. As such, it can be extended to a vast literature that uses exogenous shifts in the effective supply as an instrument to estimate demand elasticities. Typical examples are sovereign and corporate bonds and equities from both developed and emerging economies.

Second, a growing literature on inelastic financial markets emphasizes the role of the demand side in explaining asset prices across various financial markets (Koijen and Yogo, 2019; Gabaix and Koijen, 2021; Vayanos and Vila, 2021). Taking as given expected asset payoffs,

<sup>&</sup>lt;sup>1</sup>Beyond index rebalancings, Droste et al. (2023) use high-frequency U.S. Treasury auctions to estimate the effect of demand shocks on Treasury yields.

this literature analyzes how an inelastic demand affects the pricing of risk-free U.S. Treasuries (Krishnamurthy and Vissing-Jorgensen, 2012; Greenwood et al., 2015; Mian et al., 2022; Jiang et al., 2021b) and international financial assets (Koijen and Yogo, 2020; Gourinchas et al., 2022; Greenwood et al., 2023).<sup>2</sup> Similar to our study, Choi et al. (2022) analyze the effects of a downward-sloping demand on the optimal issuance of safe government bonds. In contrast, we focus on the interplay between a downward-sloping demand curve, default risk, and the provision of risky bonds.<sup>3</sup> We show that the demand elasticity interacts with default risk and influences a government's supply of risky bonds.

Third, our study also connects to a body of work examining how changes in the investor base of government debt impact bond yields (Warnock and Warnock, 2009; Dell'Erba et al., 2013; Peiris, 2013; Arslanalp and Poghosyan, 2016; Ahmed and Rebucci, 2022). In related work, Fang et al. (2022) develop a demand system to quantify how changes in the composition of investors (domestic versus foreign, banks versus non-banks) affect government bond yields in international markets. Zhou (2024) focuses on emerging market sovereign debt and shows that differences in a country's foreign investor base can help explain the heterogeneous influence of the global financial cycle. In this paper, we exploit exogenous changes in the composition of the investor base (passive versus active funds) to provide evidence of downward-sloping demand curves for risky sovereign bonds.

Fourth, our paper relates to a large literature on quantitative sovereign debt models (Aguiar and Gopinath, 2006; Arellano, 2008; Chatterjee and Eyigungor, 2012). Our framework extends standard models by introducing a downward-sloping demand for bonds, different investor types (active and passive), and secondary bond markets, which creates a tight link with our empirical analysis and allows us to discipline the model based on our reduced-form estimates. Using this setup, we show that an inelastic demand serves as a commitment device that lowers default risk. In this regard, our paper connects to a broader literature on the use of fiscal rules as commitment devices (Alfaro and Kanczuk, 2017; Dovis and Kirpalani, 2020; Hatchondo et al., 2022; Bianchi et al., 2023). We show that if the demand for bonds is inelastic, the market by itself can create incentives that discourage borrowing and decrease

<sup>&</sup>lt;sup>2</sup>A related literature focuses on U.S. and international corporate bond markets (Dathan and Davydenko, 2020; Bretscher et al., 2022; Calomiris et al., 2022; Kubitza, 2023).

<sup>&</sup>lt;sup>3</sup>Kaldorf and Rottger (2023) analyze the implications of convenience yields on the pricing and optimal supply of risky sovereign bonds. In their setup, and similarly to Choi et al. (2022), investors are willing to pay a higher price for holding risky sovereign bonds due to their collateral services. In contrast, based on our empirical results, our model assumes that investors demand a premium (an inconvenience yield) for holding risky bonds. <sup>4</sup>In this regard, our paper connects with recent work by Costain et al. (2022), who introduce endogenous default risk into a Vayanos-Vila preferred habitat model to analyze the term structure of interest rates in the European Monetary Union.

default risk.

In our analysis, we are agnostic about the mechanisms behind the downward-sloping demand. Previous work by Borri and Verdelhan (2010), Lizarazo (2013), Pouzo and Presno (2016), and Arellano et al. (2017) analyze sovereign debt models with risk-averse investors. In these models, investors are inelastic because they must be compensated for each additional unit of risky debt they hold. There are several other mechanisms that can explain a downward-sloping demand. For example, it can be driven by regulatory limitations such as a Value-at-Risk (VaR) constraint (Gabaix and Maggiori, 2015; Miranda-Agrippino and Rey, 2020), by liquidity considerations (He and Milbradt, 2014; Moretti, 2020; Chaumont, 2021; Passadore and Xu, 2022), by investors' buy-and-hold strategies, or by fixed-share mandates specifying how investors should allocate their funds across assets (as in Gabaix and Koijen, 2021). Our setup relies on a flexible demand structure that can accommodate any of these potential drivers. Our aim is not to uncover the causes of investors' inelastic behavior but rather to examine its aggregate implications.

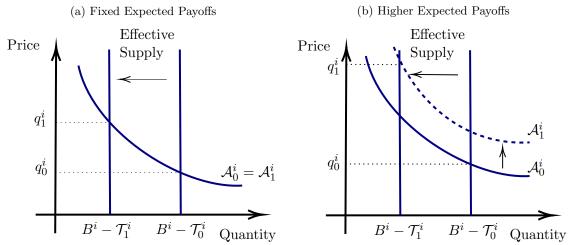
The rest of the paper is structured as follows. Section 2 introduces a simple framework to guide our analysis. Section 3 presents the empirical analysis, including details on the institutional setup of the EMBIGD index, data sources, identification strategy, and results. Section 4 formulates a sovereign debt model with endogenous default and inelastic investors, and Section 5 presents the quantitative analysis. Section 6 concludes.

# 2 Index Rebalancings as Passive Demand Shocks

We introduce a simple framework featuring active and passive investors to guide our empirical analysis. The setup follows Pavlova and Sikorskaya (2022) and illustrates how one can use index rebalancings to identify changes in the passive demand which, in turn, imply a shift in the available bond supply. These shifts can then be utilized to estimate reduced-form price demand elasticities. Although we focus on the case of sovereign bonds, the same methodology can be applied to any asset (e.g., equities).

Consider a bond i that is part of a benchmark index  $\mathcal{I}$ . Investors are heterogeneous in their degree of activism or passivism. In particular, investors track the composition of the  $\mathcal{I}$  index but differ in how actively or passively they do so. The underlying mechanism is that, due to potential tracking error costs, passive investors do not want to deviate from the composition of the index they follow. Let  $\mathbf{w}_t = \{w_t^1, ..., w_t^N\}$  denote the vector of time-varying index weights for each constituent bond of  $\mathcal{I}$ . We define the passive demand,  $\mathcal{T}_t^i(w_t^i)$ , as the portion

Figure 1 Index rebalancing and the demand elasticity



Note: The figure depicts a decrease in the effective supply driven by an increase in  $\mathcal{T}^i$ . Panel (a) considers the case when the expected payoffs do not change as a consequence of the lower effective supply. Panel (b) considers a case in which the expected payoffs increase.

of investors' holdings aimed at replicating the composition of the  $\mathcal{I}$  index. We explicitly write  $\mathcal{T}_t^i(w_t^i)$  as a function of  $w_t^i$  to emphasize its dependence on the index weights. This demand captures the holdings of both semi- and fully passive investors, it is perfectly inelastic, and shifts with changes in the index.

Let  $B^i$  denote the supply for bond i, which we assumed fixed for now. By decomposing the demand into an active and passive component, we can write the market-clearing condition for bond i as  $B^i = \mathcal{A}_t^i + \mathcal{T}_t^i\left(w_t^i\right)$ , where  $\mathcal{A}_t^i$  denotes the active demand. For any bond i in fixed supply, an increase in the passive demand implies a decrease in the supply of bonds available to active investors (i.e., a leftward shift in the effective or residual supply). If this increase is exogenous, one can use that variation to analyze whether the demand curves for active investors slope downward. Panel (a) of Figure 1 illustrates this point. If the active demand is inelastic, an exogenous increase in  $\mathcal{T}_t^i(w_t^i)$  should lead to a higher bond price.

Based on this graphical intuition, one could exploit changes in index weights  $w_t^i$  to compute shifts in the passive demand,  $\Delta \mathcal{T}_t^i \equiv \mathcal{T}_{t+1}^i(w_{t+1}^i) - \mathcal{T}_t^i(w_t^i)$ , and estimate bond price responses around those shifts,  $\Delta q_t^i$ . With this, one can then estimate the following reduced-form (inverse) demand elasticity:

$$\hat{\eta}^i = (-) \frac{\Delta q_t^i}{\Delta \mathcal{T}_t^i} \frac{B^i - \mathcal{T}_t^i}{q_t^i}.$$
 (1)

Exploiting observed variations in index weights  $w_t^i$  can still pose challenges. First, changes in  $w_t^i$  might be driven by endogenous changes in asset prices or can coincide with large issuances or redemptions. Second, the estimated price reactions in Equation (1) might capture not only an inelastic demand component but also potential (endogenous) changes in

expected payoffs. Put differently, to directly map Equation (1) into a structural elasticity  $(\eta^i)$ , we would need to assume that the intrinsic value of asset i is unaffected by the  $\Delta \mathcal{T}_t^i$  shock. However, the shock itself might influence the expected payoffs. For example, for long-term bonds, a larger  $\Delta \mathcal{T}_t^i$  may affect next-period payoffs if the shock is persistent. Moreover, the issuer can react to the shock (for instance, by increasing its supply), which may also affect the expected payoffs from holding the asset. If investors anticipate these responses, they should price them.

Panel (b) of Figure 1 provides a graphical illustration of this case. If a positive  $\Delta \mathcal{T}_t^i$  raises the next-period expected repayment, investors should be willing to pay a higher price for any given quantity of the bond, leading to an upward shift in the active demand. Failing to account for this effect might lead to the conclusion that the demand curve is steeper (more inelastic) than it truly is. Conversely, if a positive  $\Delta \mathcal{T}_t^i$  lowers the next-period expected repayment, it would cause the active demand to shift downward. This shift might lead to the demand curve being estimated as flatter (more elastic) than it truly is. Since bond prices and payoffs are jointly determined, it is challenging to disentangle the effects on bond prices due to the downward-sloping demand from those resulting from changes in expected payoffs.

Given these two challenges we proceed in two steps. In Section 3 we detail a novel identification strategy, based on index rebalancings and their timing, to estimate reduced-form elasticities for risky sovereign bonds. Then, to formally map these price reactions to structural elasticities, we formulate in Section 4 a sovereign default model in which bond prices, the bond supply, and bond payoffs are endogenous and determined simultaneously.

# 3 Empirical Analysis

#### 3.1 Identifying Exogenous Shifts in Bond Supply

We exploit end-of-month rebalancings in the J.P. Morgan EMBIGD to identify exogenous shifts in the supply of bonds available to active investors (i.e., the effective supply). The EMBIGD tracks the performance of emerging market sovereign and quasi-sovereign U.S. dollar-denominated bonds issued in international markets.<sup>5</sup> Among bond indexes for emerging economies, the EMBIGD is the most widely used as benchmark and is tracked by funds with

<sup>&</sup>lt;sup>5</sup>The index includes bonds with a maturity of at least 2.5 years and a face amount outstanding of at least US\$500 million. To be classified as an emerging economy, a country's gross national income (GNI) per capita must be below an Index Income Ceiling (IIC) for three consecutive years. The IIC is defined by J.P. Morgan and adjusted every year by the growth rate of the World GNI per capita, Atlas method (current US\$), provided by the World Bank. Bonds in the index must settle internationally and have accessible and verifiable bid and ask prices. Once included, they can remain in the index until 12 months before maturity. Local law instruments are not eligible.

combined assets under management (AUM) of around US\$300 billion in 2018 (Appendix Figure D2).<sup>6</sup> Unlike other indexes that use a traditional market capitalization-based weighting scheme, the EMBIGD limits the weights of countries with above-average debt outstanding (relative to other countries in the index) by including only a fraction of their face amount so as to achieve greater diversification. We refer to this methodology as a "cap rule".<sup>7</sup>

Rebalancings in the EMBIGD index occur on the last business day of each month in the United States and are triggered by bond inclusions and exclusions. J.P. Morgan announces these updates through a report detailing the updated index composition. As a consequence, at the end of each month, passive investors mimicking the index need to adjust their portfolios by buying or selling bonds to match the new index weights.

Following Pandolfi and Williams (2019), we construct the flows implied by the rebalancings (FIR) measure for each country c at each rebalancing date. The FIR quantitatively measures the inflows (or outflows) to each country resulting from passive investors' portfolio rebalancings, relative to the market value of the country's bonds held by active investors, and is constructed as follows:

$$FIR_{c,t} \equiv \frac{\Delta \tilde{\mathcal{T}}_{c,t}}{q_{c,t-1}B_{c,t-1} - w_{c,t-1}\mathcal{W}_{t-1}}.$$
 (2)

The  $\Delta \tilde{T}_{c,t}$  term captures the change in passive demand implied by the index rebalancing. It measures the amount of funds that, on a given rebalancing date, enter or leave a country due to the rebalancing in the portfolio of passive investors tracking the EMBIGD index. We normalize  $\Delta \tilde{T}_{c,t}$  by the market value of bonds available to active investors,  $q_{c,t-1}B_{c,t-1} - w_{c,t-1}W_{t-1}$ , where W denotes the AUM passively tracking the EMBIGD. We define the implied change in the passive demand as  $\Delta \tilde{T}_{c,t} \equiv (w_{c,t} - w_{c,t}^{BH})W_t$ . The term  $w_{c,t}$  is the benchmark weight for country c at time t. It is defined as  $w_{c,t} \equiv \frac{q_{c,t}B_{c,t}f_{c,t}}{q_tI_t}$ , where  $q_{c,t}B_{c,t}$  denotes the market value of bonds from country c at time t,  $q_{c,t}$  denotes the price, and  $B_{c,t}$  denotes the face amount outstanding. We define the diversified face amount (DFA) as  $f_{c,t}B_{c,t}$ , where  $f_{c,t}$  is the diversification coefficient, that is, the share of country c's face amount outstanding that is included in the index given the cap rule of the EMBIGD.  $f_{c,t}$  is smaller than one for

<sup>&</sup>lt;sup>6</sup>Appendix Figures D3 and D4 show that U.S. dollar-denominated bonds account for the majority of emerging economies' government debt issued in international markets.

<sup>&</sup>lt;sup>7</sup>The J.P. Morgan Emerging Markets Bond Index Global (EMBIG) has the same bond inclusion criteria as the EMBIGD. The only difference between the EMBIG and the EMBIGD is that while the former uses a market capitalization weighting scheme, the latter adopts the cap rule to limit the weights of countries with above-average debt outstanding. Appendix Figure D1 plots the country weights of both the EMBIG and EMBIGD for December 2018.

countries with greater-than-average outstanding debt.  $^8$   $q_tI_t$  denotes the market value of the EMBIGD index, where  $q_t$  is the unit price of the index and  $I_t$  is the number of available index units. Consequently,  $w_{c,t}$  is the market capitalization of country c's sovereign bonds included in the index (i.e., the DFA) relative to the total value of the index. The term  $w_{c,t}^{BH}$  denotes a "buy-and-hold weight," defined as the weight that country c would have had at time t if the index composition had remained unchanged, that is, if no bonds had entered or exited the index at time t. This weight, defined as  $w_{c,t}^{BH} \equiv w_{c,t-1} \frac{q_{c,t}/q_{c,t-1}}{q_t/q_{t-1}} = \frac{q_{c,t}f_{c,t-1}B_{c,t-1}}{q_tI_{t-1}}$ , can therefore be thought of as the weight of each country in the portfolio of an investor mimicking the index immediately before J.P. Morgan releases the end-of-month update on the composition of the EMBIGD.  $^9$ 

The FIR measure has the appealing feature of being an intuitive empirical counterpart for the term  $\frac{\Delta \tilde{\tau}}{B-T}$  in Section 2. As such, a FIR of 1% implies a 1% reduction in the supply of the country's bonds available to active investors at the time each rebalancing becomes effective. Despite this appealing feature, the FIR might not be however entirely orthogonal to changes in countries' fundamentals, for two reasons. First, the FIR is affected by countries' sovereign bond issuances. When a country issues new bonds that become part of the index (or redeems existing ones), its weight changes, leading to changes in the FIR. Second, even for countries whose  $B_{c,t}$  remains constant, the FIR can be mechanically correlated to present or past bond price changes. Given that we aim to isolate exogenous shifts in the available supply of bonds to estimate a reduced-form elasticity, the potential endogeneity of the FIR could bias our estimates.

Our empirical strategy addresses these endogeneity concerns in two ways. First, for each rebalancing event, we restrict our analysis to countries whose amount outstanding of bonds,  $B_{c,t}$ , remains unchanged relative to the previous month. In other words, we focus only on countries that do not experience new issuances, bond repurchases, or the removal of bonds from the index due to maturity on the given month.

Second, we exploit the features of the cap rule in the weighting scheme of the EMBIGD. The rule limits the face amount of a country's bonds included in the index based solely on the face amount outstanding of the bonds, and independent of their market value. This

<sup>&</sup>lt;sup>8</sup>Appendix A describes the rules that the EMBIGD uses to compute the weights of the instruments included in the index. In a purely market capitalization-weighted indexes,  $f_{c,t} = 1$  for every country that is part of the index.

<sup>&</sup>lt;sup>9</sup>Absent any change in the index composition (i.e., inclusions or exclusions of new bonds),  $w_{c,t} = w_{c,t}^{BH}$ . If the price of a country's sovereign bonds increases more than that of other countries in the index, the weight of that country in the index increases. Nevertheless, investors do not need to rebalance their portfolios as the "buy-and-hold weight" already coincides with the new weight in the index.

is crucial as it allows us to exclude the variation in the FIR that is potentially correlated with current or past bond price changes. To do so, we construct an instrument for the FIR based on a synthetic index in which country weights are only a function of the diversified face amount outstanding of bonds included in the index,  $\tilde{w}_{c,t} \equiv \frac{f_{c,t}B_{c,t}}{\sum_c f_{c,t}B_{c,t}}$ . We then compute the fractional change in the synthetic index:

$$\frac{\Delta \tilde{w}_{c,t}}{\tilde{w}_{c,t-1}} = \left(\frac{f_{c,t}B_{c,t}}{\sum_{c} f_{c,t}B_{c,t}} - \frac{f_{c,t-1}B_{c,t-1}}{\sum_{c} f_{c,t-1}B_{c,t-1}}\right) / \left[\frac{f_{c,t-1}B_{c,t-1}}{\sum_{c} f_{c,t-1}B_{c,t-1}}\right]. \tag{3}$$

Focusing on countries whose debt outstanding in the index remains unchanged  $(B_{c,t} = B_{c,t-1})$ , the instrument becomes

$$Z_{c,t} \equiv \left(\frac{f_{c,t}}{\sum_{c} f_{c,t} B_{c,t}} - \frac{f_{c,t-1}}{\sum_{c} f_{c,t-1} B_{c,t-1}}\right) / \left[\frac{f_{c,t-1}}{\sum_{c} f_{c,t-1} B_{c,t-1}}\right]. \tag{4}$$

 $Z_{c,t}$  is the fractional change in country c's weight on a synthetic index that relies solely on the face amount bonds and is therefore only affected by inclusions or exclusions of bonds, irrespective of any change in the relative market capitalization of bonds in the index. By focusing on countries with no change in debt oustanding and instrumenting the FIR with  $Z_{c,t}$ , we can isolate the variation in the available supply of a country's bonds due to passive rebalancing-driven inflows, which is orthogonal to that country's issuances or bond price changes—i.e., exogenous shifts in bond supply. Variation in  $Z_{c,t}$  is the result of changes in the size of other countries' sovereign bond markets, which produce both a direct effect on country c's weight (e.g., if the face amount of other countries fall, the relative size of country c increases) and an indirect impact through changes in the diversification coefficient  $f_{c,t}$ , which in turn depends on the average face amount of countries in the index. Within a given rebalancing date, the direct effect is proportionally the same for all countries in the index, while the indirect effect differs, as we illustrate in the following example.

## 3.2 The Rebalancing and Cap Rule in Practice

To illustrate how rebalancings and the cap rule work in practice, we consider an example involving 5 countries ( $c = \{A, B, C, D, E\}$ ) with bonds included in the index in month t - 1. For simplicity, each of these countries has only one qualifying bond and does not issue (nor redeem) bonds during month t. We assume that another country, F, issues an eligible bond for the first time during month t. This bond is therefore included in the index on the rebalancing date at the end of month t.

Table 1 shows the face amount  $FA_c$  for each country included in the index before and after the rebalancing date t. Columns  $DFA_c$  show the diversified face amount (i.e.,  $f_cB_c$ )

Table 1
The cap rule: Face amount vs diversified face amount

Country	Before R	ebalancing	After Re	ebalancing
	$\overline{FA_{c,t-1}}$	$\overline{DFA_{c,t-1}}$	$FA_{c,t}$	$\overline{DFA_{c,t}}$
A	1,000	1,000	1,000	1,000
В	2,000	2,000	2,000	2,000
$\mathbf{C}$	3,000	3,000	3,000	3,000
D	7,000	6,429	7,000	6,769
${f E}$	12,000	10,000	12,000	11,000
F	-	-	8,000	7,615
$\overline{ICA}$	5,000		5.	,500
$FA_{max}$	12	12,000		2,000

Note: The table assumes values for the face amount for each country. It then computes the diversified face amount following Equation (A1).

Table 2
Flows Implied by Rebalancing (FIR)

c	$DFA_{c,t-1}$	$DFA_{c,t}$	$q_{c,t}$	$MV_{c,t}^{BH}$	$MV_{c,t}$	$w_{c,t}$	$w_{c,t}^{BH}$	$FIR_{c,t}$
A	1,000	1,000	0.90	900	900	2.85%	3.97%	-14.43%
В	2,000	2,000	1.25	2,500	2,500	7.91%	11.03%	-16.70%
$\mathbf{C}$	3,000	3,000	0.85	2,550	$2,\!550$	8.07%	11.25%	-15.14%
D	6,429	6,769	1.20	7,714	8,123	25.72%	34.04%	-13.24%
$\mathbf{E}$	10,000	11,000	0.90	9,000	9,900	31.34%	39.71%	-10.18%
$\mathbf{F}$	-	7,615	1.00	-	7,615	24.11%	0.00%	-

Note: Market values  $MV_{c,t}^{BH}$  and  $MV_{c,t}$  are based on the diversified face amount (DFA) and bond price (q) information. They are computed as  $MV_{c,t}^{BH} \equiv DFA_{c,t-1} \times q_{c,t}$  and  $MV_{c,t} \equiv DFA_{c,t} \times q_{c,t}$ . Observed and buy-and-hold index weights are given by  $w_{c,t} = \frac{MV_{c,t}}{\sum_c MV_{c,t}}$  and  $w_{c,t}^{BH} = \frac{MV_{c,t}^{BH}}{\sum_c MV_{c,t}^{BH}}$ . The FIR measure is computed based on Equation (2), assuming a value of AUM tracking the index equal to 8,000. The assumed bond prices in period t-1 are displayed in Appendix Table D1.

calculated based on the methodology described in Appendix A. That is, the face amount included in the index after applying the cap rule of the EMBIGD for countries with above-average debt levels. In the example, countries D and E are capped in periods t-1 and t, while country F is capped in t.

Table 2 (last column) shows our FIR measure for this example. To compute the FIR, we first calculate each country's market value  $(MV_{c,t})$ , buy-and-hold market value  $(MV_{c,t}^{BH})$ , (observed) weight  $(w_{c,t})$ , and buy-and-hold weight  $(w_{c,t}^{BH})$ . The example illustrates how the FIR depends not only on the "cap rule" but also on bond prices, as evidenced by the varying FIR values among countries that are not subject to the cap (A, B, C). We do not calculate the FIR for country F, as we restrict our attention to the subset of countries whose face value remains unchanged.

Table 3 reports the theoretical weights  $\tilde{w}$ , which are only a function of the diversified face

Table 3
Heterogeneity induced by the cap rule

c	$\tilde{w}_{c,t-1} = \frac{DFA_{c,t-1}}{\sum_{c} DFA_{c,t-1}}$	$\tilde{w}_{c,t} = \frac{DFA_{c,t}}{\sum_{c} DFA_{c,t}}$	$Z_t = \frac{\tilde{w}_{c,t} - \tilde{w}_{c,t-1}}{\tilde{w}_{c,t-1}}$
A	4.46%	3.19%	-28.54%
В	8.92%	6.37%	-28.54%
$\mathbf{C}$	13.38%	9.56%	-28.54%
D	28.66%	21.57%	-24.75%
$\mathbf{E}$	44.59%	35.05%	-21.39%
$\mathbf{F}$	-	24.26%	-
_	44.59%		-21.39% -

Note: The table shows the theoretical index weights calculated based on the diversified face amount. The last column shows the percentage change in the theoretical weights, Z.

amount, and our Z instrument, computed based on Equation (4). Since we only consider countries with a constant face amount outstanding, changes in  $\tilde{w}$ , and therefore our instrument Z, are driven exclusively by country F's issuance and are uncorrelated with price changes.

This example also shows the direct and indirect effects of country inclusions on the weights of the other countries. First, the issuance of a new bond by country F and its inclusion in the index reduce the weights of all other countries. Absent the cap rule, in a purely market capitalization-based index, this direct effect would be the only one at play and would produce a relative decrease in index weights that is homogeneous across all other countries. However, the cap rule introduces variability in the relative change in the theoretical weights across countries. This variation arises because the diversified face amount (used to calculate  $\tilde{w}$ ) is capped for countries with above-average amounts of outstanding bonds, and the cap changes after the inclusion of country F.<sup>10</sup> By relaxing the cap for countries with above-average face amounts (D and E), the inclusion of country F produces a decrease in country weights that is smaller for countries with greater face amount outstanding. In the next section, we explain how we exploit this variation across countries to estimate bond price demand elasticities.

#### 3.3 Estimation Strategy

To estimate a reduced-form elasticity, we exploit the rebalancing-driven shifts in the available supply of bonds discussed in the previous section together with the timing of the EMBIGD rebalancings, which occur on the last business day of each month. More specifically, we focus on 10-day windows around each rebalancing date, distinguishing between pre- and post-rebalancing days, and estimate the average price reactions to exogenous changes in the

The inclusion of the bond from country F increases the average country face amount outstanding (ICA) from \$5,000 to \$5,500. The diversified face amounts of countries A, B, and C are unaffected because their face amounts are below the ICA. However, the increase in the ICA relaxes the cap for initially capped countries D and E, altering their diversified face amounts outstanding even though their face values remain constant.

FIR – making use of our proposed instrument, Z – around each event.<sup>11</sup>

Formally, we adopt an instrumented difference-in-differences (DDIV) design and estimate the following main specification using two-stage least squares (2SLS):

$$\log(q_{i,t,h}) = \theta_{c(i),t} + \theta_{b(i),t} + \gamma \mathbb{1}_{h \in Post} + \beta(FIR_{c(i),t} \times \mathbb{1}_{h \in Post}) + \mathbf{X}_{i,t} + \varepsilon_{i,t,h}, \tag{5}$$

where  $FIR_{c(i),t}$  are the flows implied by the rebalancing to country c in rebalancing day t, instrumented by  $Z_{c,t}$  in a first stage regression.

 $q_{i,t,h}$  is the price of bond i at rebalancing event t, h trading days before or after the rebalancing information is released. For example, h = 1 indicates the first trading day after J.P. Morgan releases the EMBIGD's new composition. This happens during the trading hours on the last business day of each month, meaning that h = 1 falls on this day. For each rebalancing event t, we consider a symmetric h-day window around it.  $\mathbb{I}_{h \in Post}$  is an indicator function equal to 1 in the h days after the rebalancing and equal to 0 in the h days before.  $\theta_{c(i),t}$  are country-month fixed effects, and  $\theta_{b(i),t}$  are bond characteristics-month fixed effects, including maturity, rating, and bond type (sovereign or quasi-sovereign).  $\mathbf{X}_{i,t}$  is a vector of monthly bond controls, including the bond's face amount and (beginning-of-month) spread. The coefficient of interest is  $\beta$ , which captures the effect of shifts in the available supply of a country's index bonds on their prices. Specifically, it measures how much a 1 p.p. exogenous rise in the FIR influences the average change in the log price of bonds around the rebalancing date.

Our preferred specification replaces the country-month fixed effects, bond characteristicsmonth fixed effects, and bond controls with bond-month fixed effects. This specification exploits both within and across rebalancing variation in  $Z_{c,t}$ . Additionally, we present results that only exploit within-event cross-country variation in  $Z_{c,t}$  by including month- $\mathbb{1}_{h \in Post}$ fixed effects.

We also estimate a leads and lags regression in which the FIR, always instrumented by Z, is interacted with trading-day dummies around the rebalancing event. This analysis allows us to both explore the dynamic effect of the FIR and test for parallel trends before the rebalancing. We estimate via 2SLS the following regression:

$$\log(q_{i,t,h}) = \theta_{c(i),t} + \theta_{b(i),t} + \sum_{h \neq -2} \gamma_h \mathbb{1}_h + \sum_{h \neq -2} \beta_h(FIR_{c(i),t} \times \mathbb{1}_h) + \mathbf{X}_{i,t} + \varepsilon_{i,t,h}, \tag{6}$$

where  $\mathbb{1}_h$  are dummy variables equal to 1 for the h trading day in our [-5:+5] estimation

<sup>11</sup> Appendix Figure D5 presents a visual representation of each rebalancing and the specific days we exploit in the estimation window

<sup>&</sup>lt;sup>12</sup>Appendix Figure D5 provides a visual timeline of these events.

window and 0 otherwise.

## 3.4 Data and Summary Statistics

We collect data from different sources to compute the FIR and our instrument. The majority of the variables used in the analysis are sourced from J.P. Morgan. However, one variable is not straightforward to measure: the AUM of funds that passively track the EMBIGD,  $W_t$ . While J.P. Morgan provides data on the amount of assets benchmarked against their indexes, it does not distinguish between passive and active funds. Additionally, even if these data were available, many active funds might passively manage a significant share of their portfolios, as highlighted by Pavlova and Sikorskaya (2022).

To compute  $W_t$ , we start with J.P. Morgan data on assets tracking the EMBIGD, which we then adjust based on an estimate of the share of passive funds. The estimation process involves the following steps. We retrieve data from Morningstar on the asset holdings of funds benchmarked against the EMBIGD and EMBI Global Core for 2016–2017.<sup>13,14</sup> For each fund, we compute their  $Passive\ Share = 100 - Active\ Share$ , where  $Active\ Share$  is the measure developed by Cremers and Petajisto (2009).<sup>15</sup> We estimate this variable at the country level, which is the level at which we compute the FIR.<sup>16</sup> This allows us to separate, even for active funds, the fraction of a fund's portfolio that behaves passively. We then compute the average  $Passive\ Share$  weighted by each fund's AUM. With this strategy, we obtain an estimated passive fund share of 50%.<sup>17</sup> We calculate the passive funds tracking the index,  $W_t$ , which we utilize to construct the FIR, by adjusting the AUM benchmarked against the EMBIGD using a rescaling factor of 50%.<sup>18</sup>

We gather data on individual bond prices from Datastream and obtain several bond characteristics (maturity and duration, among others) directly from J.P. Morgan Markets.

<sup>&</sup>lt;sup>13</sup>The EMBI Global Core uses the same diversification methodology as the EMBIGD to calculate the bond weights, as described in Appendix A. The criteria for including bonds in the EMBI Global Core is the same as that for the EMBIGD (and the EMBI Global), except the minimum face amount of the bonds must be US\$1 billion and the maturity required to be maintained in the index is of at least one year.

 $<sup>^{14}</sup>$ The sample periods utilized in the paper are determined by data access constraints.

<sup>&</sup>lt;sup>15</sup>The active share measure evaluates the degree of active management within funds. It quantifies how much the holdings of a fund differ from the benchmark index it is compared against.

<sup>&</sup>lt;sup>16</sup>We calculate the *Active Share* at the country level by using the country weights in the index and in the funds' portfolios rather than bond weights. For the portfolios, we only assign bonds to a given country if they are included in the EMBIGD. Specifically, a country's weight in a portfolio is determined by adding together the weights of all bonds from that country that are included in the EMBIGD.

<sup>&</sup>lt;sup>17</sup>Appendix Table D2 provides results using alternative shares of passive funds used to construct the FIR measure. Although our quantitative estimates change slightly, the qualitative implications remain the same. <sup>18</sup>For comparison, we also construct the *Active Share* at the bond level, and obtain a value-weighted average of 72%. Cremers and Petajisto (2009) show an average value-weighted *Active Share* that fluctuates between 55% and 80%.

Table 4 Summary statistics

Variable	Mean	Std. Dev.	25th Pctl	75th Pctl	Min	Max
$\log(\text{Price})$	4.64	0.13	4.59	4.68	3.07	5.19
Instrumented FIR (%)	-0.15	0.20	-0.32	0.00	-0.66	0.23
Stripped spread (bps)	278	288	128	356	0	4904
EIR duration (%)	6.36	3.92	3.48	7.71	-0.03	19.08
Average life (years)	9.6	8.9	4.0	9.9	1.0	99.8
Face amount (billion U.S. dollars)	1.3	0.8	0.7	1.6	0.5	7.0

Note: This table displays summary statistics for the main variables in the analysis. Stripped Spread is the difference between a bond yield-to-maturity and the corresponding point on the U.S. Treasury spot curve, where the value of collateralized flows are "stripped" from the bond. EIR Duration measures the sensitivity of dirty prices to parallel shifts of the U.S. interest rates, expressed as the percentage change of dirty price if all U.S. interest rates change by 100 basis points. Average Life is the weighted average period until principal repayment. Sources: Bloomberg, Datastream, J.P. Morgan Markets, Morningstar Direct, and authors' calculations.

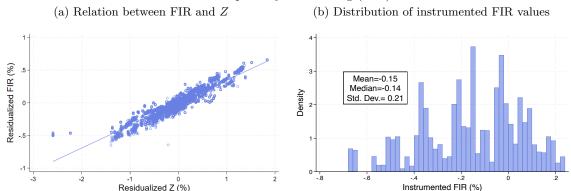
To clean our dataset, we drop extreme values of daily returns, stripped spreads, and  $Z_{c,t}$ . We drop stripped spreads below 0 or above 5,000 basis points as well as observations below the 5th or above the 95th percentiles in terms of the distribution of  $Z_{c,t}$ . The reason for the latter is that extreme values of  $Z_{c,t}$  could be driven by large, pre-announced changes in the EMBIGD and thus are not appropriate for our identification strategy, which relies on the assumption that most information is known on the last business day of the month. Finally, we exclude bond-month observations that experience daily returns below the 1st and above the 99th percentiles.

Our final dataset comprises 131,820 bond-time observations for 751 bonds in 68 countries. Table 4 displays summary statistics for our main measure of the instrumented flows implied by the rebalancing,  $FIR_{c,t}$ , as well as for the other key variables in our database. Bonds in our sample have an average stripped spread of 278 basis points, an average maturity of 10 years, and an average face amount of US\$1.3 billion.

Figure 2, Panel (a) presents the results of our first stage. It shows a scatter plot of the FIR and the  $Z_{c,t}$  instrument after both variables have been residualized with rebalancing-month and country fixed effects. The variables have a clear positive relation, and the R-squared is 86%. Panel (b) presents the distribution of our instrumented FIR measure. The values range from -0.7% to around 0.25%, with more negative than positive observations. This is consistent with the fact that over time, the number of bonds included in the EMBIGD increased. Given that we restrict our analysis to countries whose face amount remains constant, including bonds from other countries typically reduces the weight of sample countries (i.e., a negative

<sup>&</sup>lt;sup>19</sup>Stripped spread is defined in the notes of Table 4.

Figure 2 Flows implied by rebalancing (FIR)



Notes: Panel (a) presents a scatter plot of the FIR and the Z instrument. Both variables are residualized based on a regression with rebalancing-month and country fixed effects. The FIR is computed as in Equation (2) and Z as in Equation (4). Panel (b) shows a histogram of the FIR instrumented with Z. For both panels, the sample period is 2016-2018.

FIR).<sup>20</sup>

#### 3.5 Results

Table 5 reports the results of our baseline estimation using a five-day window around each rebalancing event (i.e.,  $h \in [-5, 5]$ ).<sup>21</sup> Our coefficient of interest,  $\beta$ , is always positive and statistically significant in the different specifications. The estimate in our preferred specification, with bond-rebalancing and bond-month fixed effects (column 4), implies that a 1 p.p. increase in the FIR increases bond returns by around 0.30 p.p.<sup>22</sup>

<sup>&</sup>lt;sup>20</sup>When a bond is added to the index, it generally reduces the weight of other bonds in terms of their total face amount. However, in certain situations, it could increase the weight of certain countries through a relaxation of face amount caps, as the EMBIGD sets limits on the included face amount of countries to maintain a diversified portfolio.

<sup>&</sup>lt;sup>21</sup>In Appendix Table D3 we present also the estimates obtained with simple OLS regressions of log bond prices on the FIR. In this case, the coefficients are slightly lower than in the 2SLS, consistent with a potential downward bias due to the endogeneity of the FIR measure to price changes around the rebalancing date.

<sup>&</sup>lt;sup>22</sup>In Appendix Table D4 we estimate an OLS regression with an alternative FIR that holds prices constant, using previous rebalancing period prices. Results are similar to our main estimates. Additionally, our results are robust to alternative windows around the rebalancing events (Appendix Table D5) and to excluding quasi-sovereign bonds from the analysis (Appendix Table D6).

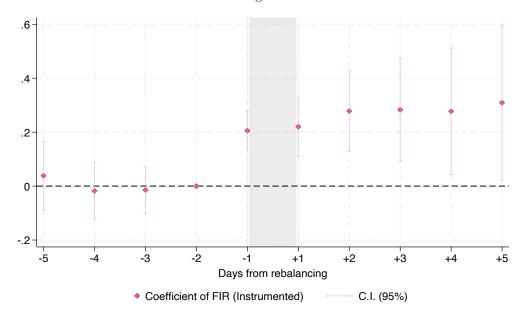
Table 5
Log price and FIR

Symn	netric wi	indow: [-	-5:+5]	Excl.	h=-1
0.006					
(0.808)					
0.231**	0.232**	0.231**	0.300**	0.263***	0.319**
(0.099)	(0.100)	(0.099)	(0.134)	(0.098)	(0.135)
0.001*	0.001*	0.001*		0.001**	
(0.000)	(0.000)	(0.000)		(0.000)	
Yes	Yes	No	No	No	No
Yes	No	No	No	No	No
No	Yes	No	No	No	No
No	Yes	No	No	No	No
No	No	Yes	Yes	Yes	Yes
No	No	No	Yes	No	Yes
No	Yes	No	No	No	No
105,548	105,508	105,548	105,548	84,433	84,433
738	738	738	738	738	738
68	68	68	68	68	68
1,576	1,575	1,576	1,576	1,576	1,576
654	1,616	1,666	476	1,670	476
	0.006 (0.808) 0.231** (0.099) 0.001* (0.000) Yes No No No No No 105,548 738 68 1,576	0.006 (0.808) 0.231** 0.232** (0.099) (0.100) 0.001* 0.001* (0.000) (0.000) Yes Yes Yes No No Yes No No No No No No No Yes 105,548 105,508 738 738 68 68 1,576 1,575	0.006 (0.808)  0.231** 0.232** 0.231** (0.099) (0.100) (0.099)  0.001* 0.001* 0.001* (0.000) (0.000)  Yes Yes No  No Yes No  No Yes No  No No Yes  No No  No Yes  No No  No Yes  No No  No Yes  No No  No Yes  No No  No Ses  No  105,548 105,508 105,548  738 738 738  68 68 68  1,576 1,575 1,576	(0.808)         0.231** 0.232** 0.231** 0.300***         (0.099) (0.100) (0.099) (0.134)         0.001* 0.001* 0.001*         (0.000) (0.000) (0.000)         Yes       No       No         No       No       No         No       Yes       No       No         No       Yes       No       No         No       Yes       No       No         No       No       Yes       Yes         No       No       Yes       No         No       Yes       No       No         105,548 105,508 105,548 105	0.006       (0.808)         0.231** 0.232** 0.231** 0.300** 0.263***         (0.099) (0.100) (0.099) (0.134) (0.098)         0.001* 0.001* 0.001* 0.001*       0.001**         (0.000) (0.000) (0.000)       (0.000)         Yes       No       No       No         No       No       Yes       Yes         No       No       Yes       Yes         No       No       Yes       No         No       Yes       No       No         105,548 105,548 105,548 105,548 105,548 84,433       738       738         68       68       68       68       68         1,576 1,576 1,576 1,576 1,576 1,576       1,576       1,576

Note: This table presents 2SLS estimates of log bond prices on the FIR measure (Equation (2)), instrumented by Z (Equation (4)), around rebalancing dates. The first- and secondstage equations are described in Equation (5). The estimations use a symmetric fivetrading-day window, with Post as an indicator variable (equal to 1 for the five trading days after rebalancing, and 0 otherwise) in Columns 1-4. Month fixed effects are dummy variables equal to 1 for each rebalancing month (0 otherwise), and bond characteristics are fixed effects that interact maturity, ratings, and bond type fixed effects. Maturity fixed effects are constructed by dividing a bond's time to maturity into four different categories: short (less than 5 years), medium (5–10 years), long (10–20 years), and very long (20+ years). Ratings from each bond are from Moody's. Bond type differentiates sovereign from quasi-sovereign bonds. Bond controls indicate whether the estimation includes the log face amount and log stripped spread of the bond. The last two columns in the analysis drops the trading day before rebalancing and the trading day h = +5 to have a four-trading-day symmetrical window around the rebalancing. Standard errors are clustered at the country-month level, and the sample period is 2016–2018. \*, \*\*, and \*\*\* denote statistically significant at the 10%, 5%, and 1% level, respectively.

One potential concern with these results is that bonds receiving a larger or smaller FIR during the rebalancings are on different price trends even before the rebalancing date. To show that this is not the case, we use the specification with leads and lags described in Equation (6). The estimated  $\beta_h$  coefficients are reported in Figure 3.

Figure 3 Leads and lags coefficients



Note: This figure presents leads and lags coefficients from a 2SLS estimation of bond log prices on a set of trading-day dummies around each rebalancing event, using the same 2SLS procedure as in Table 5. The estimation includes bond characteristics-month fixed effects (maturity, rating, and bond type). The shaded area indicates the rebalancing on the month's last business day, with h=+1 for returns on that day and h=-1 for returns on the preceding business day. The vertical red lines show a 95% confidence interval for each horizon. Standard errors are clustered at the country-month level.

On the initial four of the five trading days before the index rebalancing, changes in the FIR are not associated with systematic differences in bond prices. Instead, in the trading days after the event, the coefficient increases, becomes positive and significant, and eventually stabilizes below 0.35 by the end of our estimation window. We do observe a slight anticipation in the day before the index rebalancing, which is not uncommon in these setups. For example, this is consistent with the patterns of portfolio rebalancings by different institutional investors highlighted in Escobar et al. (2021), who show that institutional investors could move in the day before the actual index rebalancing event. In the last two columns of Table 5, we show the estimates based on our preferred specification of Equation (5) but after excluding the trading day before the index rebalancing. This leads to estimates between 0.26 and 0.32, which we take as our baseline since it does not contain any anticipation effect in the pre-period.

A related concern is the potential for additional anticipation throughout the month. Between the middle and end of every month, J.P. Morgan releases preliminary estimates about end-of-month face amounts, market values, and bond weights. While it is conceivable that active investors traded on this information before the actual index rebalancing date,

Table 6
Log price and FIR: Role of default risk

Dependent Variable: Log Price						
	High Spread					
FIR X Post	0.406***	0.406***	0.116	0.115		
	(0.147)	(0.146)	(0.097)	(0.097)		
Bond FE	Yes	No	Yes	No		
Month FE	Yes	No	Yes	No		
Bond-Month FE	No	Yes	No	Yes		
Observations	42,169	42,166	42,267	42,267		
N. of Bonds	500	500	494	494		
N. of Countries	62	62	51	51		
N. of Clusters	1,217	1,217	869	869		
F (FS)	544	1,889	421	820		

Note: This table presents 2SLS estimates of bond log prices on the FIR measure, instrumented by Z, across rebalancing dates. The sample is divided into high-spread bonds in Columns 1 and 2, above the median stripped spread, and low-spread bonds in Columns 3 and 4, below the median. The sample period and the 2SLS procedure are identical to those described in Table 5. The estimation excludes the trading day before rebalancing and the trading day h = +5 to have a four-trading-day symmetrical window around the rebalancing. The coefficients for Post and FIR are included in the estimation but not reported for brevity. Standard errors are clustered at the country-month level. \*, \*\*, and \*\*\* denote statistically significant at the 10%, 5%, and 1% level, respectively.

our data do not support this behavior. Normally, if a significant number of investors were anticipating the index rebalancing, we would expect to observe pre-trends in bond prices before the actual event. However, our analysis reveals no correlation between the FIR and bond returns in the week leading up to the rebalancing (with the only exception being the day before the event). Lastly, if part of the rebalancing-driven inflows were to occur before the event, our FIR measure would overestimate them at the index rebalancing date. This, in turn, implies that our estimates can be understood as a lower bound.<sup>23</sup>

The documented effects are heterogeneous across bonds with varying levels of default risk. To show this heterogeneity, we divide our sample into high- and low-spread bonds, those

<sup>&</sup>lt;sup>23</sup>Appendix Table D2 shows how our estimates change as we proportionally decrease the FIR measure (due to a lower share of passive funds). These results could serve as guidance for what might happen if the FIR measure were lower due to some investors' portfolio rebalancings being anticipated.

above and below the median spread in our sample, respectively. We estimate Equation (5) for each of these subsamples and report the results in Table 6. The table shows that the price of high-spread bonds is more sensitive to rebalancing shocks, with a 1 p.p. increase in the FIR associated with a 0.41 p.p. increase in bond returns. In contrast, for low-spread bonds, the effect is smaller (around 0.11 p.p.) and not statistically significant.<sup>24</sup> Overall, these findings suggest that investors demand a premium as compensation for holding risky bonds, that is, an inconvenience yield.

We can directly map the estimated bond price reactions to a reduced-form demand elasticity. Based on our FIR measure, we can rewrite Equation (1) as  $\hat{\eta} = (-)\frac{\Delta \log(q_t^i)}{FIR_{c,t}}$ , which is precisely what the  $\beta$  coefficient in Equation (5) captures. Based on the estimates in Table 5 (last columns), the inverse demand elasticity is around -0.3, implying a demand elasticity of -3. Our inverse demand elasticity estimate is higher (in magnitude) than those for sovereign bonds issued in advanced economies, but smaller relative to other asset classes, such as equities. In Appendix Figure D6, we compare our estimates with other studies.

<sup>&</sup>lt;sup>24</sup>Appendix Table D7 divides bonds into three groups according to their spreads. We find that bond prices are positively associated with the FIR for both high (above 302 basis points) and medium (between 158 and 302 basis points) spread bonds. Instead, for low spread bonds (below 158 basis points), the relationship is statistically insignificant. Additionally, the estimated coefficient increases with the risk profile of the bonds.

# 4 A Sovereign Debt Model with Inelastic Investors

We next formulate a quantitative sovereign debt model to study the impact of a downward-sloping demand on a government's supply of risky bonds. The model features a risk-averse government that lacks commitment and issues long-term debt in international debt markets. We introduce a rich demand structure, allowing us to capture a downward-sloping demand for government bonds that we discipline based on our empirical estimates.

#### 4.1 Model Setup

We consider a small open economy with incomplete markets and limited commitment. Output y is exogenous and follows a continuous Markov process with a transition function  $f_y(y_{t+1} \mid y_t)$ . Preferences of the representative consumer are given by

$$\mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t u\left(c_t\right),\tag{7}$$

where  $\beta$  is the discount factor, c denotes consumption, and the function u(.) is strictly increasing and concave.

An infinite-lived, risk-averse government issues long-term bonds in international markets. Let  $B_{t-1}$  denote the beginning-of-period stock of government debt. The government has limited commitment and can default on its debt. Each unit of B matures in the next period with probability  $\lambda$ . If a bond does not mature (and the government does not default), it pays a coupon  $\nu$ . Let  $d_t = \{0, 1\}$  denote the default policy, where d = 1 indicates a default. Default leads to a temporary exclusion from international debt markets and an exogenous output loss,  $\phi(y_t)$ . The government is benevolent and chooses  $\{d_t, B_t\}$  to maximize Equation (7), subject to the economy's resource constraint.

International markets are competitive, and investors discount payoffs at the risk-free rate. These markets are populated by a large number of heterogeneous investors (J) who differ in how they allocate their funds across bonds. As in Gabaix and Koijen (2021), we introduce a downward-sloping demand by assuming that each investor j has a mandate or rule that specifies how they should allocate their funds across the N bonds (each issued by a different country). A fraction of these investors are passive and track the composition of a benchmark bond index  $\mathcal{I}$ , of which the government's bonds (B) are part of it.

#### 4.2 Inelastic Investors

Let  $j = \{1, ..., J\}$  denote the investor. Let  $i = \{1, ..., N\}$  denote the set of bonds in which investors can invest and let  $\mathbf{w}_t = \{w_t^1, ..., w_t^N\}$  denote the vector of time-varying index weights for each constituent bond of index  $\mathcal{I}$ . We define  $x_{jt}^i = \frac{q_t^i B_{jt}^i}{W_{jt}}$  as the share of wealth that investor j invests in bond i at time t. The term  $q_t^i$  denotes the unit price of bond i,  $B_{j,t}^i$  denotes the holdings of investor j in bond i, and  $W_{j,t}$  denotes their wealth. The share  $x_{jt}^i$  is given by the following exogenous mandate:

$$x_{jt}^{i} = \theta_{j} \left( \xi_{j}^{i} e^{\Lambda_{j} \hat{\pi}_{i,t} (r_{t+1}^{i})} \right) + (1 - \theta_{j}) w_{t}^{i}, \tag{8}$$

where  $\theta_j$  parameterizes the degree of activeness or passiveness of investor j. Purely passive investors can be characterized by  $\theta_j = 0$ , indicating that their portfolio simply replicates the benchmark index  $\mathcal{I}$ . Conversely, active and semi-active investors are those with  $\theta_j \in (0, 1]$ , which captures the fraction of their portfolio that is not linked to index  $\mathcal{I}$ . Within their active allocation, investors apportion a fixed fraction,  $\xi_j^i$ , of their wealth to bond i and a varying component determined by  $\Lambda_j \hat{\pi}_{i,t} \left( r_{t+1}^i \right)$ , where  $\Lambda_j > 0$  parameterizes their demand elasticity and  $\hat{\pi}_{i,t}$  is an arbitrary function of the next-period excess return of bond i,  $r_{t+1}^i$ . For instance, if  $\hat{\pi}_{i,t} \left( r_{t+1}^i \right) = \mathbb{E}_t \left( r_{t+1}^i \right)$ , investors allocate a higher share of their wealth to bonds with higher expected excess returns.

The reduced-form mandate in Equation (8) allows us to introduce an aggregate demand elasticity for bond i that can be parameterized by  $\Lambda \equiv \{\Lambda_1, ..., \Lambda_J\}$ . While this mandate can have different microfoundations (as shown in Appendix B), we take it as given for our analysis. Our goal is not to explain the reasons behind the inelastic demand for risky bonds but rather to examine its implications. After adding up all the individual demands, we can write the market-clearing condition as follows:

$$q_t^i B_t^i = \tilde{\mathcal{A}}_t^i + \tilde{\mathcal{T}}_t^i(w_t^i), \tag{9}$$

where  $B_t^i$  is the end-of-period bond supply, and  $\tilde{\mathcal{A}}_t^i \equiv \sum_j W_{j,t} \theta_j \left( \xi_j^i e^{\Lambda_j \hat{\pi}_{i,t}} \right)$  and  $\tilde{\mathcal{T}}_t^i(w_t^i) \equiv \sum_j W_{j,t} \left( 1 - \theta_j \right) w_t^i$  denote the market-value active and passive demands, respectively. The passive demand,  $\tilde{\mathcal{T}}_t^i(w_t^i)$ , is the portion of investors' holdings aimed at replicating the index composition they follow. It captures the holdings of both semi- and fully- passive investors. We write  $\tilde{\mathcal{T}}_t^i(w_t^i)$  as a function of  $w_t^i$  to emphasize its dependence on the index weights.

We now put more structure behind the investor demand, allowing us to derive a closed-form solution for the price. We assume that  $\hat{\pi}_{i,t}(r_{t+1}^i) = \frac{\mathbb{E}_t(r_{t+1}^i)}{\mathbb{V}_t(r_{t+1}^i)}$  so that the active demand

is a function of the bond's expected excess return and its variance (the Sharpe ratio).<sup>25</sup> We define  $\mathcal{R}_{t+1}^i$  as the next-period repayment per unit of the bond so that  $r_{t+1}^i \equiv \frac{\mathcal{R}_{t+1}^i}{q_t^i} - r_f$ , where  $r_f$  denotes the risk-free rate. Based on these definitions and the market-clearing condition in Equation (9), the equilibrium bond price is given by

$$q_t^i = \frac{\mathbb{E}_t \left( \mathcal{R}_{t+1}^i \right)}{r^f} \, \Psi_t^i. \tag{10}$$

The term  $\frac{\mathbb{E}_t(\mathcal{R}_{t+1}^i)}{rf}$  captures the price under perfectly elastic investors, which is only a function of the expected next-period repayment. On the other hand, the  $\Psi_t^i$  function captures the demand's downward-sloping nature and is given by

$$\Psi_t^i \equiv 1 - \kappa_t^i \left( \mathbf{\Lambda} \right) \frac{\mathbb{V}_t \left( \mathcal{R}_{t+1}^i \right)}{\mathbb{E}_t \left( \mathcal{R}_{t+1}^i \right)} \left( B_t^i - \mathcal{T}_t^i - \bar{\mathcal{A}}_t^i \right). \tag{11}$$

The term  $\kappa_t^i(\mathbf{\Lambda}) \equiv \frac{1}{\sum_j \Lambda_j W_{j,t} \theta_j \xi_j^i}$  characterizes the elasticity of the active demand for bond i. The  $B_t^i - \mathcal{T}_t^i$  component is what we have referred to as the residual supply, and  $\bar{\mathcal{A}}_t^i$  captures the inelastic portion of the active demand, which depends on the fixed component of investors' mandates,  $\xi_j^i$  (see Appendix B for the details and derivations). Notice that when  $\kappa_t^i(\mathbf{\Lambda}) = 0$ , the active demand is perfectly elastic and the price for bond i only depends on its expected repayment. When  $\kappa_t^i(\mathbf{\Lambda}) > 0$ , the demand is inelastic and differs across bonds with different repayment variances (i.e., default risk), which is consistent with our empirical findings. We view the  $\Psi_t^i$  term as capturing an inconvenience yield, that is, a premium demanded by investors as compensation for holding the bond.

#### 4.3 Government Problem: Recursive Formulation

We focus on a Recursive Markov Equilibrium (RME) and represent the infinite horizon decision problem of the government as a recursive dynamic programming problem (see Appendix C.2 for the equilibrium definition).

We introduce the pricing equations derived in the previous subsection into the problem of the sovereign government, who issues a risky bond that is part of the index  $\mathcal{I}$ . For simplicity, we will omit the i subindex in what follows. In order to have a recursive formulation of the problem, we assume that the passive demand is given by  $\mathcal{T}' = \mathcal{T}(\tau, B')$  where B' denotes the end-of-period stock of government bonds and  $\tau$  is a (time-varying) index weight. We assume that  $\tau$  is exogenous and follows a continuous Markov process with a transition function  $f_{\tau}(\tau' \mid \tau)$ . Given an end-of-period bond supply B', the market-clearing condition can we

<sup>&</sup>lt;sup>25</sup>This is a similar specification to the one in Gabaix and Koijen (2021), which is a function of expected excess returns and a shock to tastes or perceptions of risk.

written as  $B' = \mathcal{A}'(.) + \mathcal{T}(\tau, B')$ , where  $\mathcal{A}'(.)$  denotes the (end-of-period) active demand.

Under these assumptions, the state space can be summarized by the n-tuple (h, B, s), where h captures the government's current default status, B is the beginning-of-period stock of debt, and  $s = (y, \tau)$  are the exogenous states. For a given default status h and choice of B', the resource constraint of the economy can be written as

$$c(h = 0, B, y, \tau; B') = y + q(y, \tau, B')(B' - (1 - \lambda)B) - (\lambda + (1 - \lambda)\nu)B,$$

$$c(h = 1) = y - \phi_i(y),$$
(12)

where  $q(y, \tau, B')$  denotes the price of a unit of debt,  $B' - (1 - \lambda)B$  are new bond issuances, and  $(\lambda + (1 - \lambda)\nu)B$  are current debt services.

If the government is not in default, its value function is given by

$$V(y,\tau,B) = \text{Max}_{d=\{0,1\}} \left\{ V^r(y,\tau,B), V^d(y) \right\},$$
(13)

where  $V^r(.)$  denotes the value function in case of repayment and  $V^d(.)$  denotes the default value. If the government chooses to repay, then its value function is given by the following Bellman equation:

$$V^{r}(y,\tau,B) = \operatorname{Max}_{B'} u(c) + \beta \operatorname{\mathbb{E}}_{s'|s} V(y',\tau',B'),$$
subject to  $c = y + q(y,\tau,B') \left(B' - (1-\lambda)B\right) - (\lambda + (1-\lambda)\nu) B.$ 

$$(14)$$

While in default, the country is excluded from debt markets and cannot issue new debt. The government exits a default with probability  $\theta$ , with no recovery value. We further assume that the demand from passive investors is zero while the government is in default. Under these assumptions, the value function in case of default is given by

$$V^{d}(y) = u(y - \phi(y)) + \beta \mathbb{E}_{s'|s} \left[ \theta V(y', \tau', 0) + (1 - \theta) V^{d}(y') \right].$$
 (15)

Based on the analysis in Section 4.2, given an exogenous state  $\{y, \tau\}$  we can write the bond price function that the government faces as a function of B' as follows:

$$q(y,\tau,B') = \beta^{\star} \mathbb{E}_{s'|s} \left[ \mathcal{R} \left( y',\tau',B' \right) \right] \Psi \left( y,\tau,B' \right), \tag{16}$$

where  $\beta^* \equiv 1/r_f$  is the lenders' discount factor,  $\mathcal{R}'(.) \equiv \mathcal{R}(y', \tau', B')$  denotes the next-period repayment function, and  $\Psi(y, \tau, B')$  captures the downward-sloping component of the active demand. In turn, the next-period repayment function is given by

$$\mathcal{R}\left(y',\tau',B'\right) = \left[1 - d\left(y',\tau',B'\right)\right] \left[\lambda + (1-\lambda)\left(\nu + q(y',\tau',B'')\right)\right],\tag{17}$$

where  $d(y', \tau', B')$  is the next-period default choice and  $q(y', \tau', B'')$  denotes the next-period bond price, which is a function of next-period exogenous states,  $\{y', \tau'\}$ , and the next-period debt policy,  $B'' \equiv B'(y', \tau', B')$ .

From Equations (16) and (17), it is clear that the bond price decreases with the expected default probability. Specifically, a larger B' (weakly) increases the default risk (conditional on a level of output), and thus  $q(y, \tau, B')$  (weakly) decreases in B'. The  $\Psi(y, \tau, B')$  term introduces another mechanism for the bond price to be decreasing in B': the downward-sloping demand of active investors.

When choosing its optimal debt policy, the government internalizes the effects of changes in B' on the bond price  $q(y, \tau, B')$  through both changes in the expected repayment and the downward-sloping component of the demand. Let  $\varepsilon \equiv \frac{\partial \log q(.)}{\partial \log B'}$  denote the (inverse) supply elasticity, which can be expressed as

$$\epsilon = \frac{\partial \log \mathbb{E}_{s'|s} \mathcal{R}'(.)}{\partial \log B'} + \frac{\partial \log \Psi(.)}{\partial \log B'}.$$
(18)

The first term on the right-hand side captures the elasticity of the expected repayment function with respect to the bond supply. This elasticity is typically negative because a larger B' increases default risk and reduces the expected bond payoff. The second term captures the additional decline in the bond price due to the downward-sloping demand. As we show in our quantitative analysis, this mechanism limits the government's debt and acts as a commitment device.

### 4.4 Secondary Markets and Link with Empirical Analysis

We have introduced a passive demand in the model in order to compute the same reducedform elasticity of our empirical analysis in Section 3. Notice, however, that the empirical elasticity relies on high-frequency (daily) data. Specifically, we estimated such elasticity in a short window around the rebalancing of the  $\mathcal{I}$  index. To address this frequency disconnect, we introduce secondary markets in order to capture the high-frequency nature of our empirical elasticity. In particular, we consider two instances of trading in secondary markets within a period. The timing assumption is as follows:

- 1. The endowment y is realized. Initial states are:  $\{y, \tau, B\}$
- 2. The government chooses  $d(y, \tau, B)$  and  $B'(y, \tau, B)$ .
- 3. The primary and secondary market open. Let  $q^{SM,0}(y,\tau,B')$  denote the opening price.
- 4. The next-period index weights  $\tau'$  are realized. Bond prices are updated.

# 5. The secondary market closes. Let $q^{SM,1}(y,\tau',B')$ denote the closing price.

Under this simple extension, we can compute "high-frequency" bond price reactions to exogenous changes in index weights, just as we did in our empirical setup (i.e., price changes during a rebalancing event). Notice that, the only difference between  $q^{SM,1}$  and  $q^{SM,0}$  is due to the update of  $\tau$  since both the endowment and the stock of debt are fixed while the secondary market is open. In Appendix C, we describe in detail the pricing functions under this extension. What it is important to note is that, absent secondary markets, the timing assumption is exactly the same as in the baseline model. This implies that the proposed extension nests our baseline model.

Let  $\Delta \mathcal{T}' \equiv \mathcal{T}(\tau', B') - \mathcal{T}(\tau, B')$  denote an exogenous shift in the passive demand implied by a change in index weights. Given  $\Delta \mathcal{T}'$ , and by means of simulations, we can compute the same reduced-form elasticity  $\hat{\eta}$  of our empirical analysis:

$$\hat{\eta} = (-)\frac{\Delta q}{\Delta \mathcal{T}'} \frac{B' - \mathcal{T}(\tau, B')}{q^{SM,0}(y, \tau, B')},\tag{19}$$

where  $\Delta q \equiv q^{SM,1}(y,\tau',B') - q^{SM,0}(y,\tau,B')$ . We can then use the model to decompose  $\hat{\eta}$  into a structural demand elasticity  $\eta$  and changes in expected repayment  $\alpha$ . That is,

$$\hat{\eta} = \underbrace{\left(-\right) \frac{\Delta \Psi}{\Delta \mathcal{T}} \frac{B' - \mathcal{T}(\tau, B')}{\Psi^{SM,0}(y, \tau, B')}}_{\equiv \eta} + \underbrace{\left(-\right) \frac{\Delta \mathbb{E} \mathcal{R}'}{\Delta \mathcal{T}'} \frac{B' - \mathcal{T}(\tau, B')}{\mathbb{E}_{y', \tau'|y, \tau} \mathcal{R}(y', \tau', B')}}_{= \alpha}, \tag{20}$$

where  $\Delta\Psi \equiv \Psi^{SM,1}\left(y,\tau',B'\right) - \Psi^{SM,0}\left(y,\tau,B'\right)$  is the difference in the bond price driven by the inelastic demand component before and after the new index weight  $\tau'$  is realized. Similarly,  $\Delta\mathbb{E}\mathcal{R}' \equiv \mathbb{E}_{y'|y}\mathcal{R}\left(y',\tau',B'\right) - \mathbb{E}_{y',\tau'|y,\tau}\mathcal{R}\left(y',\tau',B'\right)$  captures the change in the bond's expected repayment once the new  $\tau'$  is realized.

There are two mechanisms underlying  $\mathbb{E}\mathcal{R}'$  that are worth emphasizing. First, if the  $\tau$  process is persistent, an increase in  $\tau$  today will have an effect on future  $\Psi$  (.) terms and, thus, on future prices and expected payoffs (as shown in Equations 16 and 17). Second, through its effects on current and future bond prices, changes in  $\tau$  affect the government's value function  $V^r(.)$  (Equation 14) and thus influence its debt and default policies, B'(.) and d(.), respectively. Changes in these policies, in turn, impact expected payoff and the bond price (Equations 16 and 17). These two mechanisms are interconnected, since chances in B'(.), for instance, may significantly impact future  $\Psi$  (.) terms. In summary, part of the price reaction captured in  $\hat{\eta}$  is reflecting these endogenous forces rather than a downward-sloping demand component.

# 5 Quantitative Analysis

#### 5.1 Calibration

We calibrate the model at a quarterly frequency using data on Argentina, a benchmark case commonly studied in the sovereign debt literature. The calibration follows a two-step procedure. We first fix a subset of parameters to standard values in the literature or based on historical Argentine data. We then internally calibrate the remaining parameters to match relevant moments for Argentine spreads and other business cycle statistics.

In terms of functional forms and stochastic processes, we assume that the government has CRRA preferences:  $u(c) = \frac{c^{1-\gamma}}{1-\gamma}$ , where  $\gamma$  denotes the risk aversion. Output follows an AR(1) process given by  $\log(y') = \rho_y \log(y) + \epsilon'_y$ , with  $\epsilon'_y \sim N(0, \sigma_y)$ . If the government defaults, output costs are governed by a quadratic loss function  $\phi(y) = \max\{d_0y + d_1y^2, 0\}$ . For  $d_0 < 0$  and  $d_1 > 0$ , the output cost is zero whenever  $0 \le y \le -\frac{d_0}{d_1}$  and rises more than proportionally with y when  $y > -\frac{d_0}{d_1}$ . This loss function is identical to the one used in Chatterjee and Eyigungor (2012) and allows us to closely match the sovereign spreads observed in the data. As for the demand of passive investors, we assume that it is proportional to the (end-of-period) amount of bonds outstanding. Specifically,  $\mathcal{T}' = \mathcal{T}(\tau, B') = \tau \times B'$ . We let  $\tau$  follow an AR(1) process given by  $\log(\tau') = (1 - \rho_\tau) \log(\tau^*) + \rho_\tau \log(\tau) + \epsilon'_\tau$ , where  $\epsilon'_\tau \sim N(0, \sigma_\tau)$ .

Based on the analysis in Section 4.2, we consider the following functional form for the downward-slopping  $\Psi(.)$  term:

$$\Psi\left(y,\tau,B'\right) = \exp\left\{-\kappa \frac{\mathbb{V}_{s'|s}\left(\mathcal{R}'(.)\right)}{\mathbb{E}_{s'|s}\left(\mathcal{R}'(.)\right)} \times \left(B' - \mathcal{T}' - \bar{\mathcal{A}}\right)\right\},\tag{21}$$

where  $\kappa \geq 0$  characterizes the elasticity of the demand function and  $\bar{\mathcal{A}}$  denotes the average holdings of active investors (as determined by the fixed component of their mandates,  $\xi_j^i$ ). For tractability, we assume time-invariant values for both  $\kappa$  and  $\bar{\mathcal{A}}$ . This specification introduces a wedge in the price of risky bonds (i.e., those with  $\mathbb{V}_{s'|s}(\mathcal{R}'(.)) > 0$ ). As we show next, it allows us to capture the two key features of our empirical analysis: a downward-sloping demand for active investors and a demand elasticity that increases (in magnitude) with default risk.

Table 7 lists the calibrated parameters. For the subset of fixed parameters (Panel a), we set  $\gamma = 2$ , which is a standard value for risk aversion in the literature. We also set a quarterly

<sup>&</sup>lt;sup>26</sup> As shown in Section 4.2, these terms could be, in principle, time-varying functions. We also use an exponential specification purely for computational reasons: to avoid having a negative price.

Table 7
Calibration of the model

	Panel a: Fixed Parameters		Panel b: Calibrated Parameters		
Param.	Description	Value	Param.	Description	Value
$\gamma$	Risk aversion	2.00	β	Discount rate	0.949
r	Risk-free interest rate	0.01	$ar{d}_0$	Default cost—level	-0.24
$\lambda$	Debt maturity	0.05	$\bar{d}_1$	Default cost—curvature	0.29
z	Debt services	0.03	$\kappa$	Slope parameter	60.0
$\theta$	Reentry probability	0.0385	$ar{\mathcal{A}}$	Active investors demand	0.526
$ ho_{ m y}$	Output, autocorrelation	0.93			
$\sigma_{ m y}$	Output, shock volatility	0.02			
$ au^\star$	Share of passive demand	0.123			
$ ho_{ au}$	FIR, autocorrelation	0.66			
$\sigma_{ au}$	FIR, shock volatility	0.02			

risk-free rate of  $r_f = 0.01$ , in line with the average real risk-free rate observed in the United States. The probability of re-entering international markets is set to  $\theta = 0.0385$ , implying an average exclusion duration of 6.5 years. We set  $\lambda = 0.05$  to target a debt maturity of 5 years and  $\nu = 0.03$  to match Argentina's average debt services. The parameters for the endowment process,  $\rho_y$  and  $\sigma_y$ , are based on log-linearly detrended quarterly real GDP data of Argentina. All these parameters are taken from Morelli and Moretti (2023). Last, we set  $\tau^*$  to match the average share of Argentina's external debt tracked by passive investors, and calibrate  $\rho_\tau$  and  $\sigma_\tau$  to match the persistence and volatility of our FIR measure.

We internally calibrate the remaining parameters (Table 7, Panel b). We jointly calibrate the default cost level and curvature,  $\{d_0, d_1\}$ , together with the government's discount factor  $\beta$ , to target Argentina's average ratio of (external) debt to GDP, average spread, and volatility of spreads.<sup>27</sup> Additionally, we calibrate  $\kappa$  to match the estimated (inverse) reduced-form demand elasticity,  $\hat{\eta}$ . Last, we set  $\bar{A}$  to match the average holdings of active investors. That is,  $\bar{A} = \bar{B} - \bar{T}$ , where  $\bar{B}$  denotes the average debt stock and  $\bar{T}$  denotes passive investors' average holdings. Given Equation (21), this is equivalent to targeting an average  $\Psi(.)$  of one, which implies that the (in)convenience yield is zero on average. The introduction of  $\Psi(.)$  thus only affects the sensitivity of the pricing kernel to changes in B' around the  $\{\bar{B}, \bar{T}, \bar{A}\}$  point.

Figure 4 depicts the default set and the bond price function q(.) for different values of B' and y. Panel (a) shows that the government defaults in states with high debt and low output. Panel (b) shows that, as a consequence, the bond price is decreasing in B' and increasing in y. The dashed lines in Panel (b) show the bond prices under a counterfactual in which we

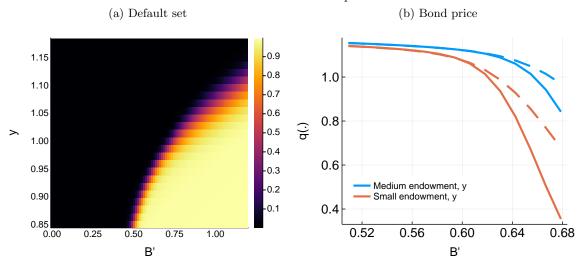
<sup>&</sup>lt;sup>27</sup>Annualized spreads are computed as  $SP = \left(\frac{1+i\left(y,\tau,B'\right)}{1+r_f}\right)^4 - 1$ , where  $i\left(y,\tau,B'\right)$  is the internal quarterly return rate, which is the value of i(.) that solves  $q\left(y,\tau,B'\right) = \frac{\left[\lambda+(1-\lambda)\nu\right]}{\lambda+i\left(y,\tau,B'\right)}$ .

Table 8
Targeted moments

Target	Description	Data	Model
$\mathbb{E}[SP]$	Bond spreads	472bp	462bp
$\sigma(SP)$	Volatility of spreads	200bp	145bp
$\mathbb{E}[D/Y]$	Debt to output	55%	62%
$\mathbb{E}[\Psi]$	Inconvenience yield	1.0	1.005
$\hat{\eta}$	Reduced-form elasticity	-0.30	-0.31

Note: The table reports the moments targeted in the calibration and their model counterpart.

Figure 4 Default set and bond prices



Note: Panel (a) shows the default policy for different combinations of B' and y. The black area depicts combinations of B' and y such that default probability is zero. Lighter colors indicate a higher default probability. In Panel (b), the solid lines show the bond pricing kernel  $q(y, \tau, B')$  for different values of B' and for two values of output. The dashed lines show the bond price under a perfectly elastic demand, taking as given the same bond and repayment policies as in our baseline model (i.e.,  $q(.)/\Psi(.)$ ).

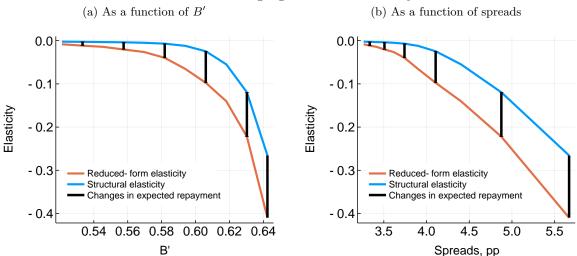
take the baseline B'(.) policy but assume that the demand is perfectly elastic (i.e., it shows the  $q(.)/\Psi(.)$  function). At lower B' levels, where default risk is minimal, bond prices remain largely unaffected by the downward-sloping demand. However, as B' increases, increased return volatility decreases  $\Psi$ , subsequently lowering the bond price q.

#### 5.2 Decomposing the Reduced-form Demand Elasticity

We formally disentangle the different channels through which changes in  $\mathcal{T}$  affect bond prices. As shown in Equation (20), index rebalancing affects bond prices through two mechanisms: (i) the (inverse) structural demand elasticity of active investors,  $\eta$ , and (ii) changes in expected repayment,  $\alpha$ . Using the calibrated model, we can isolate the effects driven by changes in expected repayment to properly identify the structural demand elasticity.

Figure 5 decomposes the channels outlined in Equation (20). The black line shows the

Figure 5 Disentangling the demand elasticity



Note: The figure shows the reduced-form inverse demand elasticity  $\hat{\eta}$  (black lines) and the structural one  $\eta$  (blue lines). The vertical differences between the two lines (represented by the red lines) capture the endogenous changes in bonds' expected repayment,  $\alpha$ . Panel (a) shows the results as a function of B', while Panel (b) shows the results as a function of annualized bond spreads.

Table 9
Persistence of shocks and demand elasticity

Moment	Baseline	Lower persistence	Low persistence	Higher persistence
Reduced-form $\hat{\eta}$	-0.31	-0.26	-0.29	-0.35
Structural $\eta$	-0.19	-0.2	-0.19	-0.18
Bias, $1 - \eta/\hat{\eta}$	41%	25%	34%	48%

Note: The table compares the reduced-form inverse demand elasticity  $\hat{\eta}$  with the structural one  $\eta$ . The "Baseline" column shows the elasticities under our baseline calibration. In the "Lower persistence" case, we decrease the persistence of the  $\{\tau\}$  process by setting  $\rho_{\tau} = 0.50$ . The "Higher persistence" column shows the results for  $\rho_{\tau} = 0.80$ .

reduced-form (inverse) demand elasticity  $\hat{\eta}$ , while the blue line depicts the model-implied structural elasticity,  $\eta$ . The vertical differences between these two curves (red lines) indicate the portion of the reduced-form elasticity attributable to endogenous changes in the repayment function,  $\alpha$ . We find that the magnitude of  $\hat{\eta}$  is always higher than that of  $\eta$ . The difference can be substantial, particularly for larger values of B' and for higher bond spreads. The first column of Table 5 shows the unconditional average for both the reduced-form elasticity,  $\hat{\eta}$ , and the structural elasticity,  $\eta$ . On average, the structural elasticity accounts for less than two-thirds of the reduced-form elasticity.

The magnitudes of the documented biases critically depend on the persistence of the  $\tau$  process. The last two columns of Table 9 compare the reduced-form and structural elasticities for different persistence values for the  $\{\tau\}$  process (i.e.,  $\rho_{\tau}$ ). When the process is more (less) persistent, a smaller (larger) share of the total price response is accounted by the inelastic component of the investors' demand. In Appendix C.3, we analyze these biases in more detail.

Table 10 Comparison with perfectly elastic case: Unconditional moments

Moment	Description	Baseline	Perfectly elastic
$\mathbb{E}(SP)$	Bond spreads	462bp	817bp
$\sigma\left(SP\right)$	Volatility of spreads	145bp	456bp
$\mathbb{E}\left(B/y\right)$	Debt to output	62%	59%
$\mathbb{E}\left(d ight)$	Default frequency	3.73%	4.39%
$\sigma(B)/\sigma(y)$	Standard deviation of debt, relative to output	1.41	1.99
$\rho(SP, y)$	Correlation between spreads and output	-0.78	-0.57

Note: The table compares a set of key moments between our baseline model with inelastic investors and a counterfactual scenario in which investors are perfectly elastic ( $\kappa = 0$ ).

Overall, our analysis highlights the importance of accounting for issuers' endogenous responses to an exogenous (supply-shifting) shock and the resulting changes in assets' expected repayment. Neglecting these factors can introduce significant biases into the estimated demand elasticity, particularly if the shock is persistent. As argued in Section 3, our FIR measure is inherently more temporary than other supply-shifting instruments used in the literature, such as index additions or deletions. However, even in that case, the bias can represent over one-third of the reduced-form elasticity.

#### 5.3 Implications of a Downward-sloping Demand

As shown in Equation (18), in determining its optimal debt policy, the government internalizes not only the effects of a higher B' on q(.) through changes in its default probability but also its effects through the inelastic demand. This section quantifies the implications of a downward-sloping demand on bond prices, default risk, and government policies. To this end, we compare our downward-sloping demand model with an alternative scenario where investors are perfectly elastic.

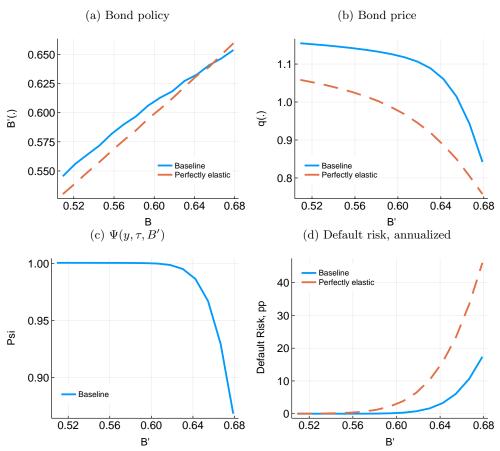
Table 10 reports a set of targeted and untargeted moments for our baseline model and for an alternative case with a perfectly elastic demand ( $\kappa = 0$ ). All the other model parameters remain the same. Despite similar values of debt, we find that the default frequency and average spreads are *lower* relative to the perfectly elastic case when facing an inelastic demand.

Two factors explain the lower default rate and bond spreads. First, the government debt policy is significantly affected by a downward-sloping demand. Panel (a) of Figure 6 shows the optimal debt policy  $B'(y, \tau, B)$  in our baseline model and in the perfectly elastic case. For large values of B (in states where  $\mathbb{V}(\mathcal{R}'(.))$  is high), an additional unit of B' reduces the bond price g(.) due to both higher default risk and investors' inelastic behavior. As a

result, the government does not find it optimal to issue large amounts of debt because it is too costly to do so. An inelastic demand thus introduces a limit to the maximum amount of debt that a government is willing to issue.

Second, these changes in the optimal bond policy have important effects on the pricing of bonds (Figure 6, Panel (b)). For small values of B' (low default risk), q(.) is actually higher than under the perfectly elastic case. As shown in Panel (c), this larger bond price is not driven by a convenience yield because, given our calibration,  $\Psi(.)$  is typically smaller than one. Instead, the higher bond price is explained by a lower default risk (Panel (d)), which is a direct consequence of the government's lower incentives to issue large values of B'.

 $Figure \ 6 \\ Comparison \ with \ perfectly \ elastic \ case: \ Policy \ functions \ and \ prices$ 



Note: The top panel presents bond policies and prices as a function of B. We evaluate all the functions at the mean value for output, y. Blue solid lines show the results for our baseline model with inelastic investors and the orange dashed lines shows the results in an alternative model in which investors are perfectly elastic. The bottom panel depicts the  $\Psi(y,\tau,B')$  function and the annualized default risk.

Overall, an inelastic demand diminishes a government's incentives to issue additional units of debt, acting as a commitment device that reduces default risk and increases bond prices.

How does an inelastic demand affect the optimal government response to shocks? It is

well-known that in models with limited commitment and endogenous default, the optimal bond policy is pro-cyclical (Arellano, 2008). While the government would like to issue debt more in "bad" times (i.e., when output is low) to smooth its consumption, the resulting increase in spreads, due to higher default risk, leads the government to actually decrease its debt. On the other hand, in "good" times (when output is high and default risk is low), the government benefits from cheaper credit and increases its debt issuances. This standard mechanism in sovereign debt models explains the well-known excess volatility of consumption in emerging markets.

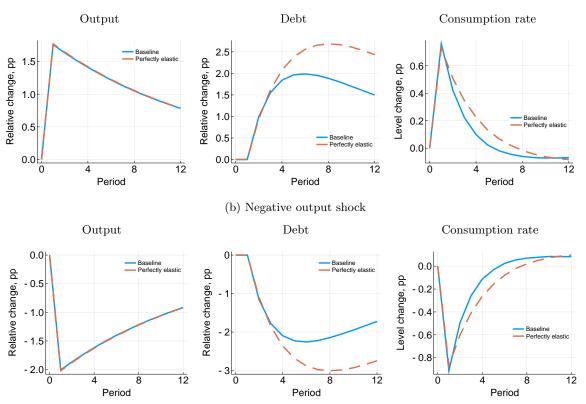
We find that this pro-cyclicality is dampened in the presence of inelastic investors. In Figure 7, we analyze the impulse responses to endowment shocks. For a positive shock (Panel a), the figure shows a higher increase in debt issuance when investors are perfectly elastic. Under a perfectly elastic demand, the government can take full advantage of the lower financing costs due to the implied decrease in default risk. Under inelastic demand, however, the government response is muted since it internalizes that, despite the cheaper financing, an additional unit of debt decreases bond prices due to the downward-sloping demand. In this sense, the inelasticity of the demand imposes a cost: it prevents the government from issuing more in periods in which debt is cheap. The right panel shows a smaller increase in the consumption rate (c/y) under inelastic demand. For a negative shock (Panel b), the story is analogous. A lower output increases borrowing costs, and the government finds it optimal to decrease its debt. Under an inelastic demand, however, reducing the stock of debt decreases the inconvenience yield demanded by investors, which lowers spreads; hence, the contraction in debt is muted.

Overall, the previous analysis implies that the government debt policy is less responsive to shocks. Figure 8 compares the unconditional distribution for the debt-to-output ratios between our baseline model and the perfectly elastic case. Under an inelastic demand, this distribution is significantly less dispersed (Panel a). In fact, the standard deviation of debt is about 30% smaller under inelastic investors (as shown in Table 10). In line with the impulse response dynamics, the debt-to-output ratio exhibits a smaller unconditional correlation with output when investors are inelastic (Panel b). This, in turn, leads to a larger correlation (in magnitude) between spreads and output (Table 10).

We conclude our analysis by examining the welfare implications of an inelastic demand. We define the certainty equivalent consumption (CEC) as the proportional increase in consumption under the perfectly elastic case, such that the household is indifferent between

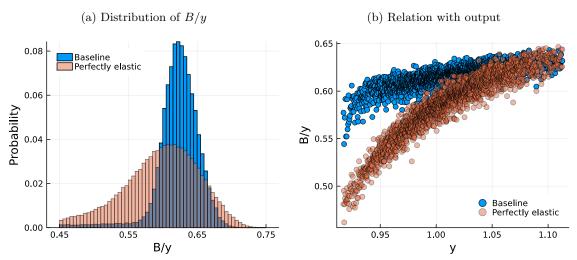
Figure 7 Impulse responses to an output shock

#### (a) Positive output shock



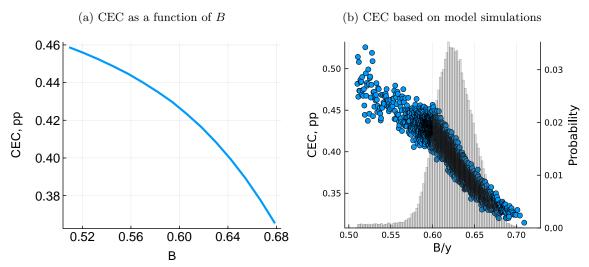
Note: Figure shows the impulse response dynamics to a positive (panel a) and negative (panel b) endowment shock. Blue lines show the dynamics for our baseline model with inelastic investors. The orange lines show the perfectly elastic case.

Figure 8 Stock of sovereign debt under inelastic investors



Note: Panel (a) shows the model simulated distributions for debt-to-output. Panel (b) shows a binscatter plot between the debt-to-output ratio and output. Blue bars and dots are for the baseline model with inelastic investors. Orange bars and dots are for an alternative model in which investors are perfectly elastic.

Figure 9 Inelastic investors: Welfare analysis



Note: Figure shows the CEC defined as the proportional increase in consumption under the perfectly elastic counterfactual such that the household is indifferent between that case and the inelastic one. Panel (a) shows the CEC across different levels of B. The blue dots in Panel (b) show the the relation between the CEC and debt-to-output ratio B/y, based on model simulations. The gray bars show the histogram for the distribution of B/y.

that scenario and the inelastic one.<sup>28</sup> Figure 9 shows the results. We find a positive CEC, which implies that the commitment device is strong enough so that the household prefers a world with inelastic investors. The CES decreases with a larger stock of debt, due to the large inconvenience yield demanded by investors (as shown in Figure 6).

## 6 Conclusion

In this paper, we present evidence of downward-sloping demand curves in risky sovereign debt markets and analyze their implications for the optimal supply of sovereign bonds. Our approach combines evidence from high-frequency bond-level price reactions to well-identified shocks with a structural model featuring endogenous debt issuances and default risk. This methodology allows us to isolate endogenous changes in expected bond payoffs behind the estimated price reactions and to back out a structural demand elasticity. Empirically, we find that a 1 p.p. exogenous reduction in the effective bond supply leads to a 30 basis point increase in bond prices. Our structural model reveals that over one-third of this response is due to endogenous changes in the expected repayment of bonds. We show that an inelastic demand can have important macroeconomic effects. In particular, we find that the inelastic demand influences and shapes the governmental policies on optimal debt and default. By

The CEC is implicitly defined as the value of  $\tilde{x}$  such that  $\sum_{t=0}^{\infty} \beta^t \mathbb{E}_t u(c_t) = \sum_{t=0}^{\infty} \beta^t \mathbb{E}_t u((1+\tilde{x})\,\tilde{c}_t)$ , where  $c_t$  denotes the consumption under an inelastic demand and  $\tilde{c}_t$  denotes the consumption under a perfectly elastic case. Exploiting the power utility function, the CEC is given by:  $\tilde{x} = \left[\frac{V(y,\tau,B)}{\tilde{V}(y,\tau,B)}\right]^{\frac{1}{1-\gamma}} - 1$ , where  $\tilde{V}(.)$  is the government's value function under the perfectly elastic case.

diminishing the government's incentives to issue additional units of debt, an inelastic demand acts as a commitment device that reduces default risk and borrowing costs. Moreover, we find that the pro-cyclicality of the debt policy is dampened in the presence of inelastic investors.

Our results highlight the importance of considering issuers' endogenous responses and the resulting changes in expected asset payoffs. Failing to account for these responses can introduce significant biases when estimating demand elasticities, particularly for risky assets. Our paper can lead to further research along several dimensions. For example, given the model predictions, it would be interesting to empirically study the impact of inelastic demand on government debt issuances. More importantly, our framework can be extended to other assets and markets, notably equity and corporate bonds. The endogenous responses that we emphasize in this paper can be applied to other issuers' of risky assets, which we leave for future research.

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## A Diversification Methodology

Relative to a market capitalization-weighted index, the EMBIGD employs a diversification methodology to produce a more even distribution of country weights. This ensures that countries with large market capitalization do not dominate the index. To achieve this goal, the methodology restricts the weights of countries with above-average debt levels by including only a portion of their outstanding debt.

The methodology is anchored on the average country face amount in the index, called Index Country Average (ICA), and defined as:

$$ICA_t = \sum_{c=1}^{C} \frac{FA_{c,t}}{C},$$

where  $FA_{c,t}$  denotes country c's bond face amount included in the index at time t, and C denotes the number of countries in the index.

The diversified face amount for any country in the index is derived according to the following rule:

- 1. The maximum threshold is determined by the country with the largest face amount  $(FA_{max})$ , capped at twice the ICA  $(ICA \times 2)$ .
- 2. If a country's face amount is between the ICA and  $FA_{max}$ , its diversified face amount is linearly interpolated.
- 3. If a county's face amount is below the ICA, the entire face amount is eligible for inclusion.

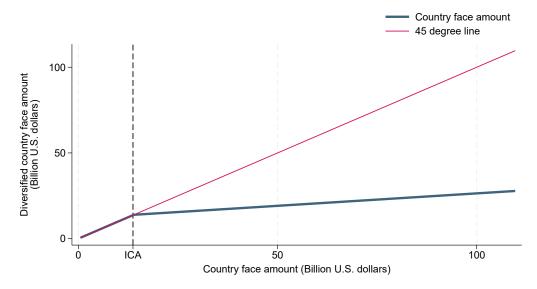
The diversified country face amount  $(DFA_{c,t})$  is calculated as follows:

$$DFA_{c,t} \begin{cases} ICA_t \times 2 & \text{if } FA_{c,t} = FA_{max,t} \\ ICA_t + \frac{ICA_t}{FA_{max_t} - ICA_t} \left( FA_{c,t} - ICA_t \right) & \text{if } FA_{c,t} > ICA_t \\ FA_{c,t} & \text{if } FA_{c,t} \leq ICA_t \end{cases}$$
(A1)

For countries with a restricted face amount in the EMBIGD, the proportional decrease applied to the country-level face amount is also applied to their respective bonds. The diversified market value is calculated by multiplying the diversified face amount by the bond price. The diversified weight of each bond is determined by its share of the total diversified market capital in the index.

Additionally, country weights are capped at 10%. Any excess weight above this cap will be redistributed pro rata to smaller countries below the cap, across all bonds from countries not capped at 10%. Appendix Figure A1 compares the country-level diversified and non-diversified face amount for December 2018.

Appendix Figure A1 Effect of the diversification methodology on the country face amount



Note: The figure illustrates the differences between the country-level face amount and their diversified versions, which the EMBIGD uses to generate the diversified bond weights. The data used are from December 2018. Sources: J.P. Morgan Markets, and authors' calculations.

## B Appendix: A Model of Inelastic Investors

In this appendix, we first provide additional material and derivations for the analysis in Section 4.2. We then describe microfoundations for the assumed demand structure, analyzing two related cases. In the first one, the inelasticity comes from investor risk aversion, while the second case is rooted in a Value-at-Risk (VaR) constraint to which investors are subject.

## **B.1** Additional Derivations

From Equation (8) in the main text, and based on a first-order approximation for the elastic component of the demand  $e^{\kappa_j\hat{\pi}_{i,t}}$  around  $\bar{\pi}_i$ , we can write the market-value demand of active investors as follows:

$$\tilde{\mathcal{A}}_t^i = \sum_j (1 - \Lambda_j \bar{\pi}_i) W_{j,t} \theta_j \xi_j^i e^{\Lambda_j \bar{\pi}_i} + \hat{\pi}_{i,t} \sum_j \Lambda_j W_{j,t} \theta_j \xi_j^i e^{\Lambda_j \bar{\pi}_i}.$$
(B1)

The first term captures investors' average purchases of bond i, which are given by their exogenous mandates  $\xi_j^i$ . The second term captures deviations from those purchases (i.e., the elastic component of the demand), which is a function of  $\hat{\pi}_{i,t}$ .

For the remainder of the analysis, we focus on the case in which  $\hat{\pi}_{i,t}\left(r_{t+1}^i\right) = \frac{\mathbb{E}_t\left(r_{t+1}^i\right)}{\mathbb{V}_t\left(r_{t+1}^i\right)}$ . Define  $\mathcal{R}_{t+1}^i$  as the next-period repayment per unit of the bond so that  $r_{t+1}^i \equiv \frac{\mathcal{R}_{t+1}^i}{q_t^i} - r_f$ , where  $r_f$  denotes the risk-free rate. We can then write  $\hat{\pi}_{i,t}\left(r_{t+1}^i\right) = q_t^i \frac{\mathbb{E}_t\mathcal{R}_{t+1}^i - q_t^i r_f}{\mathbb{V}_t\mathcal{R}_{t+1}^i}$ . Without loss of generality, consider a case where  $\bar{\pi}_i$  is close to zero. After substituting these expressions into the equation, we can rewrite Equation (B1) as follows:

$$\tilde{\mathcal{A}}_t^i = q_t^i \bar{\mathcal{A}}_t^i + q_t^i \left( \frac{\mathbb{E}_t \mathcal{R}_{t+1}^i - q_t^i r_f}{\mathbb{V}_t \mathcal{R}_{t+1}^i} \right) \sum_j \Lambda_j W_{j,t} \theta_j \xi_j^i, \tag{B2}$$

where  $\bar{\mathcal{A}}_t^i$  is defined such that  $q_t^i \bar{\mathcal{A}}_{t+1}^i = \sum_j W_{j,t} \theta_j \xi_j^i$ . We can interpret  $\bar{\mathcal{A}}_t^i$  as active investors' holdings aimed at satisfying the fixed part of their mandates.

As for the demand of passive investors, let  $M_t$  denote the market value of the index  $\mathcal{I}$  and define  $S_t^i$  as bond i's face amount included in this index. For simplicity, assume that bond i is only included in index  $\mathcal{I}$ . Then,  $w_t^i = \frac{S_t^i q_t^i}{M_t}$ , and we can write the market-value passive demand as

$$\tilde{\mathcal{T}}_{t}^{i} = q_{t}^{i} S_{t}^{i} \sum_{j} \frac{W_{j,t} (1 - \theta_{j})}{M_{t}} = q_{t}^{i} \mathcal{T}_{t}^{i},$$
(B3)

where  $\mathcal{T}_t^i \equiv S_t^i \sum_j \frac{W_{j,t}(1-\theta_j)}{M_t}$  denotes the face amount of bond i's passive holdings.

After replacing Equations (B2) and (B3) in the market-clearing condition (Equation (9)

in the main text), we obtain a closed-form solution for the bond price:

$$q_t^i = \frac{\mathbb{E}_t \left( \mathcal{R}_{t+1}^i \right)}{r_f} \left[ 1 - \kappa_t^i \frac{\mathbb{V}_t \left( \mathcal{R}_{t+1}^i \right)}{\mathbb{E}_t \left( \mathcal{R}_{t+1}^i \right)} \left( B_t^i - \mathcal{T}_t^i - \bar{\mathcal{A}}_t^i \right) \right], \tag{B4}$$

where  $\kappa_t^i(\mathbf{\Lambda}) \equiv \frac{1}{\sum_j \Lambda_j W_{j,t} \theta_j \xi_j^i}$  parameterizes the downward-slopping behavior of the demand. It is a weighted average of investors'  $\{\Lambda_j\}$  parameters, where the weights are given by the amount that each investor allocates on bond i.

Next, we show that we can obtain an analogous pricing kernel under risk-averse investors or under risk-neutral investors subject to a standard VaR constraint.

#### B.2 Microfoundation Based on Risk-Averse Investors

Consider a case where investors are risk averse and have mean-var preferences. They care about both the total return of their portfolio and their return relative to a benchmark index  $\mathcal{I}$  they track. Additionally, they are heterogeneous and differ in their degree of risk aversion and how their compensation depends on their total and relative return. Following the same notation as in the main text, let  $j = \{1, ..., J\}$  denote the investor type. Let  $i = \{1, ..., N\}$  denote the set of bonds that are part of the  $\mathcal{I}$  index, and let  $\boldsymbol{w}_t = \{w_t^1, ..., w_t^N\}$  be the vector of index weights for each constituent bond. The vector  $\boldsymbol{r}_{t+1} = \{r_{t+1}^1, ..., r_{t+1}^N\}$  denotes the next-period (gross) returns (i.e., the bond gross return in excess of the risk-free rate,  $r^f$ ). Last, let  $\boldsymbol{B}_t = \{B_t^1, ..., B_t^N\}$  denote the bond supply.

For an investor j, their total compensation is a convex combination between the return of their portfolio and the relative return versus the index  $\mathcal{I}$ . Let  $\boldsymbol{x}_{j,t} = \left\{x_{j,t}^1, ..., x_{j,t}^N\right\}$  be investor j's vector of portfolio weights. The investor's compensation is

$$TC_{j,t} = \theta_j (\boldsymbol{x}_{j,t})' \cdot \boldsymbol{r}_{t+1} + (1 - \theta_j) (\boldsymbol{x}_{j,t} - \boldsymbol{w}_t)' \cdot \boldsymbol{r}_{t+1}$$
$$= [\boldsymbol{x}_{j,t} - (1 - \theta_j) \boldsymbol{w}_t]' \cdot \boldsymbol{r}_{t+1},$$

where  $\theta_i$  captures the weight of relative returns on the compensation.

Each investor chooses a combination of portfolio weights  $\boldsymbol{x}_{j,t}$  to maximize  $\mathbb{E}_t\left(TC_{j,t}\right) - \frac{\sigma_j}{2}\mathbb{V}_t\left(TC_{j,t}\right)$ , where  $\sigma_j$  captures the investor's risk aversion. In matrix form, we can write this problem as follows:

$$\operatorname{Max}_{\boldsymbol{x}_{j}} \left[ \boldsymbol{x}_{j,t} - (1 - \theta_{j}) \boldsymbol{w}_{t} \right]' \boldsymbol{\mu}_{t} - \frac{\sigma_{j}}{2} \left[ \boldsymbol{x}_{j,t} - (1 - \theta_{j}) \boldsymbol{w}_{t} \right]' \boldsymbol{\Sigma}_{t} \left[ \boldsymbol{x}_{j,t} - (1 - \theta_{j}) \boldsymbol{w}_{t} \right],$$

where  $\mu_t \equiv \mathbb{E}_t(\mathbf{r}_{t+1})$  denotes the expected excess return of the portfolio and  $\Sigma_t \equiv \mathbb{V}_t(\mathbf{r}_{t+1})$  denotes the variance-covariance matrix of excess returns. The optimal portfolio allocation for

investor j is given by

$$\boldsymbol{x}_{j,t} = \frac{1}{\sigma_j} \boldsymbol{\Sigma}_t^{-1} \boldsymbol{\mu}_t + (1 - \theta_j) \, \boldsymbol{w}_t.$$
 (B5)

The first term on the right-hand side of Equation (B5) captures the usual mean-variance portfolio. An analogous expression can also be derived under CARA preferences (see, e.g., Pavlova and Sikorskaya, 2022). The second term reflects the reluctance of some investors to deviate from the benchmark portfolio,  $\boldsymbol{w}$ , indicating an inherently inelastic demand. It is not a function of the expected return or riskiness of the bonds; rather, it depends only on how much investors penalize deviations from the benchmark. Purely passive investors (i.e., those with  $\theta_j = 0$  and  $\sigma_j \to \infty$ ) never deviate from the benchmark portfolio and exhibit a perfectly inelastic demand.

Let  $W_{j,t}$  denote the wealth of each type of investor j. Then  $B_{j,t}^i = \frac{W_{j,t}x_{j,t}^i}{q_t^i}$  are investor j's purchases of bond i, where  $q_t^i$  denotes the bond price. For each bond i, its market-clearing condition is  $q_t^i B_t^i = \sum_j W_{j,t} x_{j,t}^i$ . After replacing these with the investors' optimal portfolio weights, the market-clearing conditions are given by

$$\begin{bmatrix} q_t^1 B_t^1 \\ \vdots \\ q_t^N B_t^N \end{bmatrix} = \sum_j W_{j,t} \left[ \frac{1}{\sigma_j} \boldsymbol{\Sigma}_t^{-1} \boldsymbol{\mu}_t + (1 - \theta_j) \boldsymbol{w}_t \right]$$

$$= \tilde{\boldsymbol{\mathcal{A}}}_t + \tilde{\boldsymbol{\mathcal{T}}}_t,$$
(B6)

where  $\tilde{\mathcal{A}}_t \equiv \sum_j W_{j,t} \frac{1}{\sigma_j} \boldsymbol{\Sigma}_t^{-1} \boldsymbol{\mu}_t$  denotes the active component of investors' demand (at market value). Since investors are risk averse,  $\tilde{\mathcal{A}}_t^i$  is downward sloping and is a function of the expected return of bond i and its variance-covariance matrix. The term  $\tilde{\mathcal{T}}_t \equiv \boldsymbol{w}_t \sum_j W_{j,t} (1 - \theta_j)$  denotes the passive demand (at market value).

Take the market-clearing condition of Equation (B6), and assume for simplicity only two assets. For ease of exposition, consider that bond i is risky and bond -i is not. Under these assumptions, the price for bond i is given by

$$q_t^i = \frac{\mathbb{E}_t \left( \mathcal{R}_{t+1}^i \right)}{r^f} \times \Psi_t^i, \tag{B7}$$

where  $\mathcal{R}_{t+1}^i$  denotes the bond's next-period repayment per unit and  $\Psi_t^i$  captures the downward-sloping nature of the demand.  $\Psi_t^i$  is given by

$$\Psi_t^i \equiv 1 - \kappa_t^{\text{RA}} \frac{\mathbb{V}_t \left( \mathcal{R}_{t+1}^i \right)}{\mathbb{E}_t \left( \mathcal{R}_{t+1}^i \right)} \left( B_t^i - \mathcal{T}_t^i \right), \tag{B8}$$

where  $1/\kappa_t^{\text{RA}} \equiv \sum_j \frac{W_{j,t}}{\sigma_j}$  denotes the weighted-average risk aversion coefficient and  $\mathcal{T}_t^i \equiv \tilde{\mathcal{T}}_t^i/q_t^i$ 

denotes the (face amount) holdings of passive investors.

Note that the bond price in Equation (B8) is analogous to the one in Equation (B4). The key difference is that with risk-averse lenders, the price elasticity is captured only by investors' risk aversion. In our main analysis, we do not specify the underlying mechanism driving this elasticity.

#### B.3 Microfoundation Based on a VaR Constraint

An identical expression can also be derived for investors who are risk neutral and subject to a VaR constraint. These constraints are common both in the literature and in the regulatory sphere (e.g., Miranda-Agrippino and Rey, 2020).<sup>29</sup>

Consider an analogous setup to the one in the previous subsection. Investors are heterogeneous and care about their absolute and relative return with respect to index  $\mathcal{I}$ . They are also risk neutral and subject to a VaR constraint that imposes an upper limit on the amount of risk they can take. In particular, the problem for investor j can be written as

$$\begin{aligned} \operatorname{Max}_{\left\{x_{j,t+1}^{1}, \dots, x_{j,t+1}^{N}\right\}} & \mathbb{E}_{t} \Big( \left[ \boldsymbol{x}_{j,t+1} - \left(1 - \alpha_{j}\right) \boldsymbol{s}_{t+1} \right]' \cdot \boldsymbol{r}_{t+1} \Big) \\ & \text{subject to} & \Phi^{2} \mathbb{V}_{t} \Big( \left[ \boldsymbol{x}_{j,t+1} - \left(1 - \alpha_{j}\right) \boldsymbol{s}_{t+1} \right]' \cdot \boldsymbol{r}_{t+1} \Big) - 1 \leq 0, \end{aligned}$$

where the parameter  $\Phi^2$  captures the intensity of the risk constraint. We view  $\Phi^2$  as a regulatory parameter that limits the amount of risk that an investor can take. Let  $\varrho_j$  denote the Lagrange multiplier associated with the VaR constraint. It can be shown that the optimal portfolio is given by

$$\boldsymbol{x}_{j,t} = \frac{1}{\varrho_j \Phi^2} \boldsymbol{\Sigma}_t^{-1} \boldsymbol{\mu}_t + (1 - \theta_j) \, \boldsymbol{w}_t. \tag{B9}$$

The previous optimal portfolio is identical to that of Equation (B5), with the only difference being that the risk-aversion parameter  $\sigma$  has been replaced by the product of the Lagrange multiplier  $\varrho_j$  and the regulatory parameter  $\Phi^2$ . Following the same steps as before, we can then derive an analogous pricing kernel to that of Equations (B7) and (B8). That is,

$$q_t^i = \frac{\mathbb{E}_t \left( \mathcal{R}_{t+1}^i \right)}{r^f} \left[ 1 - \kappa_t^{\text{VaR}} \frac{\mathbb{V}_t \left( \mathcal{R}_{t+1}^i \right)}{\mathbb{E}_t \left( \mathcal{R}_{t+1}^i \right)} \left( B_t^i - \mathcal{T}_t^i \right) \right], \tag{B10}$$

where  $1/\kappa_t^{\text{VaR}} \equiv \sum_j \frac{W_{j,t}}{\lambda_j \overline{\Phi}^2}$  denotes the (weighted-average) intensity for which the VaR constraint binds in the aggregate.

<sup>&</sup>lt;sup>29</sup>Adrian and Shin (2014) provide a microfoundation for VaR constraints. Gabaix and Maggiori (2015) use a similar constraint, in which a financier's outside option is increasing in the size and variance of its balance sheet.

## C Appendix: Quantitative Model

In this appendix, we provide additional details for the quantitative model of sections 4 and 5.

#### C.1 Secondary Markets

The empirical elasticity computed in Section 3 exploits exogenous variation in the passive demand in a small window around announcement about changes in the EMBIGD index weights. To tightly link our model with the empirical analysis, our baseline model in Section 4 already incorporates a passive demand and exogenous changes in index weights,  $\tau$ . There is, however, a frequency disconnect in the sense that the model is calibrated at quarterly frequency so it is not suitable to quantify high-frequency price reactions to changes in  $\tau$ .

To address this frequency disconnect, we introduce in the model secondary markets in which bonds trade. This, allows us to capture the high-frequency nature of our empirical elasticity. We consider two instances of trading in secondary markets within a period: before and after the new index weights,  $\tau'$  are realized. The timing assumption is as follows:

- 1. The endowment y is realized. Initial states are:  $\{y, \tau, B\}$
- 2. The government chooses  $d(y, \tau, B)$  and  $B'(y, \tau, B)$ .
- 3. The primary and secondary market open. Let  $q^{SM,0}(y,\tau,B')$  denote the opening price.
- 4. The next-period index weights  $\tau'$  are realized.
- 5. The secondary market closes. Let  $q^{SM,1}\left(y,\tau',B'\right)$  denote the bond closing price.

The first trading instance  $(SM_0)$  is at the beginning of the period, just after the government announces its default and debt choices. The bond price in this instance is given by

$$q^{SM,0}(y,\tau,B') = \beta^* \mathbb{E}_{y',\tau'|y,\tau} \mathcal{R}\left(y',\tau',B'\right) \Psi^{SM,0}\left(y,\tau,B'\right). \tag{C1}$$

The term  $\mathbb{E}_{y',\tau'|y,\tau}\mathcal{R}(y',\tau',B')$  is the expected next-period repayment of the bond, conditional on the information available when the secondary market opens. Following the derivation in Section 4.2 (see Equation (11)), the downward-sloping component of the price function is

$$\Psi^{SM,0}(y,\tau,B') = 1 - \kappa_0 \frac{\mathbb{V}_{\{y',\tau'\}|\{y,\tau\}} \mathcal{R}(y',\tau',B')}{\mathbb{E}_{\{y',\tau'\}|\{y,\tau\}} \mathcal{R}(y',\tau',B')} \left(B' - \mathcal{T}(\tau,B') - \bar{\mathcal{A}}\right)$$
(C2)

Notice that  $q^{SM,0}(y,\tau,B')$  coincides with the price in the primary market  $q(y,\tau,B')$ , which is the price relevant to the government.

The second trading instance  $(SM_1)$  occurs at the end of the period, when the secondary markets closes and after the new index weights  $\tau'$  are realized. In this case, the bond price is

$$q^{SM,1}\left(B',y,\tau'\right) = \beta^{\star} \mathbb{E}_{y'|y} \mathcal{R}\left(y',\tau',B'\right) \Psi^{SM,1}\left(y,\tau',B'\right). \tag{C3}$$

The term  $\mathbb{E}_{y'|y}\mathcal{R}(y',\tau',B')$  is the expected next-period repayment of the bond, conditional on the information available when the secondary market closes. This term is analogous to the one in Equation (C1), but incorporates the information provided by the realization of  $\tau'$ . Similarly, the downward-sloping component of the price function is given by

$$\Psi^{SM,1}\left(y,\tau',B'\right) \equiv 1 - \kappa_0 \frac{\mathbb{V}_{y'|y}\mathcal{R}\left(y',\tau',B'\right)}{\mathbb{E}_{y'|y}\mathcal{R}\left(y',\tau',B'\right)} \left(B' - \mathcal{T}\left(\tau',B'\right) - \bar{\mathcal{A}}\right). \tag{C4}$$

Notice that, the only difference between  $q^{SM,1}$  and  $q^{SM,0}$  is due to the update of  $\tau'$  since both the endowment and the stock of debt are fixed while the secondary market is open. Moreover, absent secondary markets, the timing assumption is exactly the same as in the baseline model.

#### C.2 Definition of Equilibrium

A Recursive Markov Equilibrium is a collection of value functions  $\{V(\cdot), V^r(\cdot), V^d(\cdot)\}$ ; policy functions  $\{d(\cdot), b'(\cdot)\}$ ; and bond prices  $q(\cdot)$  such that:

- 1. Taking as given the bond price function q(.), the government's policy functions  $b'(\cdot)$  and  $d(\cdot)$  solve the optimization problem in Equations (13), (14), and (15), and  $V(\cdot)$ ,  $V^{r}(\cdot)$ , and  $V^{d}(\cdot)$  are the associated value functions.
- 2. Given  $b'(\cdot)$  and  $d(\cdot)$ , the next-period repayment function  $\mathcal{R}'(\cdot)$  satisfies Equation (17).
- 3. Taking the repayment function as given, bond prices q(.) are consistent with Equation (16).

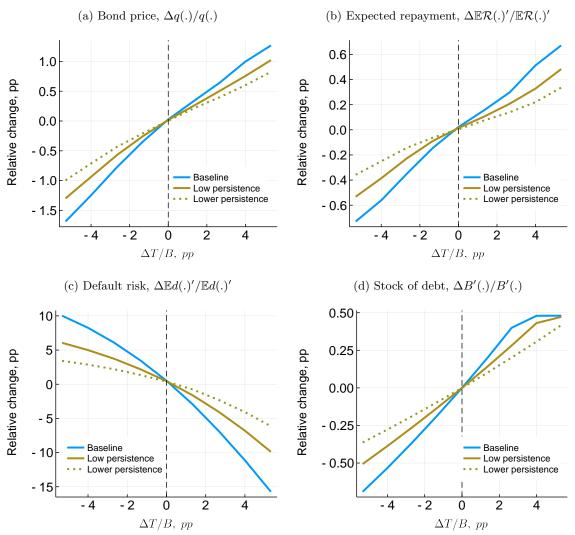
#### C.3 Understanding the Source of the Biases

What does explain the difference between the reduced-form and structural elasticity? To answer this question, we analyze the mechanisms behind changes in the expected repayment function due to a change in  $\tau$ .

The first three panels of Figure C1 show the "high-frequency" effects (i.e., changes within the same period) of shifts in the passive demand on bond prices, expected repayment, default risk, and debt. To this end, we shock  $\tau'$ , and analyze the responses of bond prices, expected repayment, and default risk from the opening to the closing of the secondary market.<sup>30</sup> The blue lines shows the results under our baseline parameterization. The solid and dotted brown lines show the results for cases in which the  $\tau$  process is less persistent. Panels (a) and (b) show that there is a monotone relation between changes in the passive demand and bond

 $<sup>\</sup>overline{}^{30}$ In all cases, we evaluate these changes at the mean value for endowment y and end-of-period debt B'.

Appendix Figure C1 Effects of Changes in demand on prices and policies



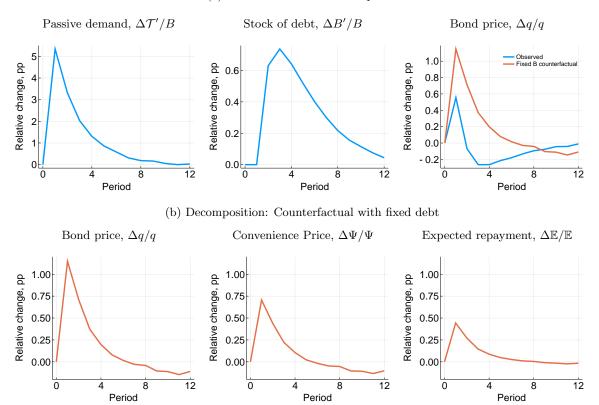
Note: The figure shows how changes in the passive demand (i.e., FIR) affect bond prices, expected repayment, default risk, and the bond supply. The blue lines show results under our baseline calibration. The brown lines show results for parameterizations in which we decrease the persistence of the FIR. For these cases, we set  $\rho_{\tau} = 0.50$  and  $\rho_{\tau} = 0.25$ .

prices and expected repayment. For a 5% increase in the passive demand (as a share of the total stock of debt), bond prices increase by almost 1.5% and about 40% of that increase is explained by an increase in the bonds' expected repayment. Panel (c) shows the change in one-period ahead default risk. For a 5% increase in the passive demand, default risk decreases about 15%. As the persistence of the  $\tau$  process decreases, the implied changes on bond prices, expected repayment, and default risk decrease. For the "lower persistence" case, for instance, default risk almost does not change, even for large shifts in the passive demand.

Panel (d) shows that the government reacts to the  $\tau'$  shock (one period after the shock). In particular, the government finds it optimal to increase its stock of debt in response to an increase in the passive demand. The response, however, is rather small: for every 1% increase

# Appendix Figure C2 Impulse response to an increase in the passive demand

(a) Effects on debt and bond prices



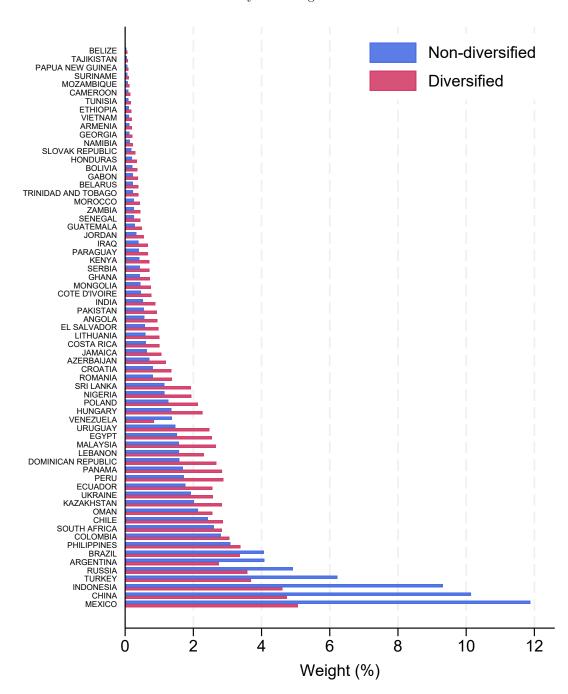
Note: The top panel shows impulse responses to an increase in the passive demand. The bottom panel shows a decomposition for bond price changes across time, in a counterfactual in which the stock of debt remains fixed.

in the passive demand (as a share of the stock of debt), the government increases its debt by 0.10%.

To shed further light on the dynamics of debt and default, Figure C2b shows the impulse response to an increase in the passive demand. The top panel shows the responses for debt and bond prices. Even though the government increase its debt, bond prices still increase as the result of the larger demand. The orange line shows a counterfactual in which we keep the bond policy fixed. In this case, the bond price increases about 40% more on impact. The bottom panel decomposes the change in bond prices for the counterfactual in which debt is fixed.

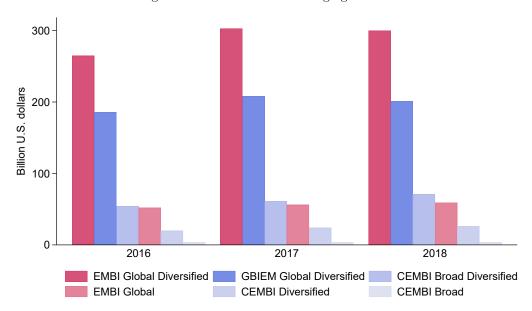
## D Appendix: Additional Figures and Tables

 ${\bf Appendix\ Figure\ D1}$  EMBI Global country-level weights in December 2018



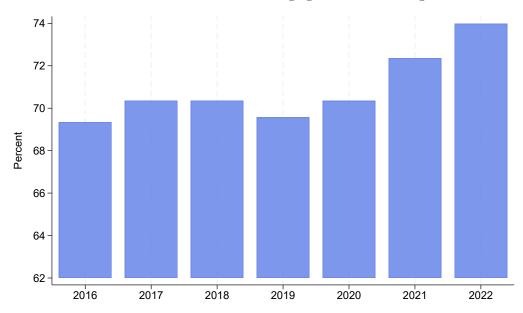
Note: The figure illustrates the EMBI Global country-level diversified and non-diversified weights for December 2018. Country-level weights are computed as the sum of the weights of all bonds from each country included in the index. Sources: J.P. Morgan Markets, and authors' calculations.

 ${\bf Appendix\ Figure\ D2}$  Assets under management benchmarked to emerging economies bond indexes



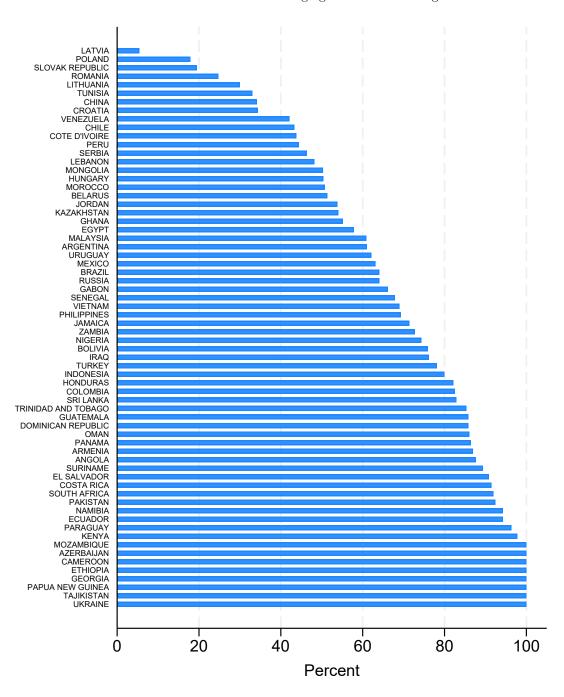
Note: The figure shows assets under management, in billions of U.S. dollars, benchmarked to emerging economies bond indexes. Sources: J.P. Morgan Markets, and authors' calculations.

 ${\bf Appendix\ Figure\ D3}$  Share of U.S. dollar-denominated emerging economies sovereign debt

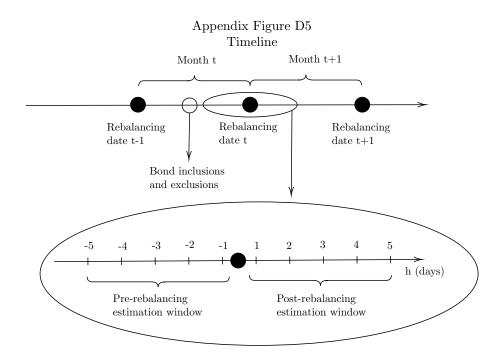


Note: The bars show the U.S. dollar-denominated sovereign debt in the EMBI Global index as a percentage of each country's general government debt securities issued in international markets. Averages are derived by calculating this percentage for each country and year, and then averaging these values annually across countries. Each country's percentage is weighted by its debt amount outstanding included in the EMBI Global indexes. Sources: BIS, J.P. Morgan Markets, and authors' calculations.

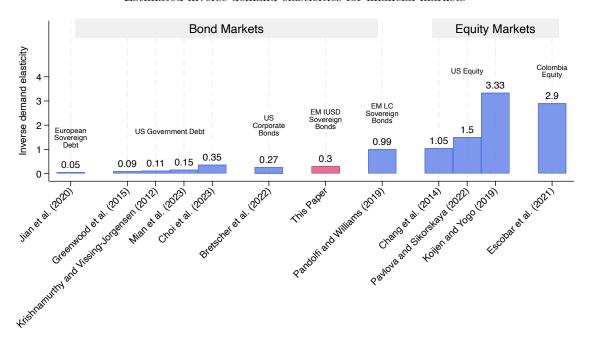
 ${\bf Appendix\ Figure\ D4}$  Share of U.S. dollar-denominated emerging economies sovereign debt



Note: The bars show the U.S. dollar-denominated sovereign debt in the EMBI Global index as a percentage of each country's general government debt securities issued in international markets. The averages are derived by calculating this percentage for each country and year, and then averaging these values across the years 2016–2022. Sources: BIS, J.P. Morgan Markets, and authors' calculations.



Appendix Figure D6 Estimated inverse demand elasticities for financial markets



Note: EM IUSD Sovereign Bonds stands for emerging economies sovereign bonds issued internationally in U.S. dollars, while EM LC Sovereign Bonds stands for those issued in local currency. The elasticities in Jiang et al. (2021a), Krishnamurthy and Vissing-Jorgensen (2012), and Greenwood et al. (2015) are taken from the review Table 2 of Mian et al. (2022) and are converted into an inverse demand price elasticity, assuming a duration of 7 for the average bond. For Choi et al. (2022), we take the midpoint elasticity from the IV estimates, while for our paper, we compute the midpoint in elasticity from Table 5. For the emerging economies local currency sovereign bonds, we take the estimated number in Table 15, Panel D of Pandolfi and Williams (2019) for GBI bonds, which we adjust by the share of AUM (23.6%) that behave de facto in a passive way. For that, we compute the asset share in EPFR tracking the GBI-EM Global Diversified with an  $R^2$  exceeding that of ETFs tracking the same index. We determine the average  $R^2$  for ETFs by using a weighted average (based on assets) of the  $R^2$  of the ETFs.

Appendix Table D1 Flows Implied by Rebalancing (FIR)

c	$FA_{c,t-1}$	$DFA_{c,t-1}$	$q_{c,t-1}$	$MV_{c,t-1}$	$w_{c,t-1}$	$w_{c,t}$	$w_{c,t}^{BH}$	$FIR_{c,t}$
A	1,000	1,000	1.00	1,000	4.72%	2.85%	3.97%	-14.43%
В	2,000	2,000	1.20	2,400	11.34%	7.91%	11.03%	-16.70%
$\mathbf{C}$	3,000	3,000	0.90	2,700	12.75%	8.07%	11.25%	-15.14%
D	7,000	$6,\!429$	1.10	7,071	33.40%	25.72%	34.04%	-13.24%
$\mathbf{E}$	12,000	10,000	0.80	8,000	37.79%	31.34%	39.71%	-10.18%
$\mathbf{F}$	-	-	-	-	-	24.11%	0.00%	-

Note: The diversified face amount  $(DFA_{c,t-1})$  is computed following Equation (A1). The market value  $(MV_{c,t-1})$  is based on the diversified face amount and bond price information,  $MV_{c,t-1} \equiv DFA_{c,t-1} \times q_{c,t-1}$ . Observed and buy-and-hold index weights are given by  $w_{c,t} = \frac{MV_{c,t}}{\sum_c MV_{c,t}}$  and  $w_{c,t}^{BH} = \frac{MV_{c,t}^{BH}}{\sum_c MV_{c,t}^{BH}}$ . The FIR measure is computed based on Equation (2), assuming a value of AUM tracking the index equal to 8,000.

Appendix Table D2 Log price and FIR: varying the share of passive funds

Dependent Variable: Log Price								
	25%	30%	35%	40%	45%			
FIR X Post	0.547***	0.442**	0.367**	0.310**	0.266**			
	(0.190)	(0.188)	(0.156)	(0.132)	(0.114)			
Bond-Month FE	Yes	Yes	Yes	Yes	Yes			
Observations	105,548	105,548	105,548	105,548	105,548			
N. of Bonds	738	738	738	738	738			
N. of Countries	68	68	68	68	68			
N. of Clusters	1,576	1,576	1,576	1,576	1,576			
F (FS)	419	1,862	1,813	1,764	1,715			

Note: This table presents 2SLS estimates of log bond prices on the FIR measure (defined in Equation (2)), instrumented by Z (defined in Equation (4)), around rebalancing dates. The first-and second-stage equations are described in Equation (5). The estimations use a symmetric five-trading-day window, with Post as an indicator variable (equal to 1 for the five trading days after rebalancing, and 0 otherwise). Each different column indicates the share of passive funds used to construct the FIR face amount measure. Month fixed effects are dummy variables equal to 1 for each rebalancing month, and 0 otherwise. Standard errors are clustered at the country-month level, and the sample period is 2016-2018. \*, \*\*\*, and \*\*\* denote statistically significant at the 10%, 5%, and 1% level, respectively.

Appendix Table D3 Log price and FIR: OLS

Dependent Variable: Log Price						
		[-5:+5]			No h= $-1$	
Post	0.000*	0.001*	0.000*		0.001**	
	(0.000)	(0.000)	(0.000)		(0.000)	
FIR	1.160*					
	(0.643)					
FIR X Post	0.197***	0.198**	0.197***	0.134	0.236***	0.167*
	(0.076)	(0.077)	(0.076)	(0.086)	(0.076)	(0.092)
Bond FE	Yes	Yes	No	No	No	No
Month FE	Yes	No	No	No	No	No
Bond Characteristics-Month FE	No	Yes	No	No	No	No
Country-Month FE	No	Yes	No	No	No	No
Bond-Month FE	No	No	Yes	Yes	Yes	Yes
Month-Post FE	No	No	No	Yes	No	Yes
Bond Controls	No	Yes	No	No	No	No
Observations	$105,\!548$	105,508	$105,\!548$	105,548	84,433	84,433
N. of Bonds	738	738	738	738	738	738
N. of Countries	68	68	68	68	68	68
N. of Clusters	1,576	1,575	1,576	1,576	1,576	$1,\!576$

Note: This table presents OLS estimates of log bond prices on the FIR measure (Equation (2)), around rebalancing dates. The estimations use a symmetric five-trading-day window, with *Post* as an indicator variable (equal to 1 for the five trading days after rebalancing, and 0 otherwise). Month fixed effects are dummy variables equal to 1 for each rebalancing month (0 otherwise), and bond characteristics are fixed effects that interact maturity and ratings fixed effects. Maturity fixed effects are constructed by dividing a bond's time to maturity into four different categories: short (less than 5 years), medium (5–10 years), long (10–20 years), and very long (20+ years). Ratings from each bond are from Moody's. Bond controls indicate whether the estimation includes the log face amount and log stripped spread of the bond. Standard errors are clustered at the country-month level, and the sample period is 2016–2018. \*, \*\*\*, and \*\*\* denote statistically significant at the 10%, 5%, and 1% level, respectively.

Appendix Table D4 Log price and FIR Constant Prices: OLS

Dependent Variable: Log Price						
		[-5:-	+5]		No h	=-1
Post	0.001*	0.001*	0.001*		0.001**	
	(0.000)	(0.000)	(0.000)		(0.000)	
FIR	1.112*					
	(0.644)					
FIR X Post	0.230***	0.232***	0.231***	0.142*	0.266***	0.177*
	(0.075)	(0.076)	(0.075)	(0.086)	(0.075)	(0.092)
Bond FE	Yes	Yes	No	No	No	No
Month FE	Yes	No	No	No	No	No
Bond Characteristics-Month FE	No	Yes	No	No	No	No
Country-Month FE	No	Yes	No	No	No	No
Bond-Month FE	No	No	Yes	Yes	Yes	Yes
Month-Post FE	No	No	No	Yes	No	Yes
Bond Controls	No	Yes	No	No	No	No
Observations	105,548	105,508	105,548	105,548	84,433	84,433
N. of Bonds	738	738	738	738	738	738
N. of Countries	68	68	68	68	68	68
N. of Clusters	1,576	1,575	1,576	1,576	1,576	1,576

Note: This table presents OLS estimates of log bond prices on a variation of the FIR measure from Equation (2), around rebalancing dates. This alternative measure holds prices constant when computing benchmark weights using the previous rebalancing period prices. The estimations use a symmetric five-trading-day window, with *Post* as an indicator variable (equal to 1 for the five trading days after rebalancing, and 0 otherwise). Month fixed effects are dummy variables equal to 1 for each rebalancing month (0 otherwise), and bond characteristics are fixed effects that interact maturity and ratings fixed effects. Maturity fixed effects are constructed by dividing a bond's time to maturity into four different categories: short (less than 5 years), medium (5–10 years), long (10–20 years), and very long (20+ years). Ratings from each bond are from Moody's. Bond controls indicate whether the estimation includes the log face amount and log stripped spread of the bond. Standard errors are clustered at the country-month level, and the sample period is 2016–2018. \*, \*\*\*, and \*\*\* denote statistically significant at the 10%, 5%, and 1% level, respectively.

Appendix Table D5 Log price and FIR: different windows

Panel A-Dependent Variable: Log Price							
	[-2:+2]	[-3:+3]	[-4:+4]	[-5:+5]			
FIR X Post	0.146***	0.197***	0.221**	0.231**			
	(0.053)	(0.071)	(0.086)	(0.099)			
Bond-Month FE	Yes	Yes	Yes	Yes			
Observations	42,217	63,327	84,435	105,548			
N. of Bonds	738	738	738	738			
N. of Countries	68	68	68	68			
N. of Clusters	$1,\!576$	$1,\!576$	1,576	1,576			
F (FS)	1,660	1,662	1,664	1,666			
Panel B-Depend	ent Varia	ble: Log	Price (E	xcl. h=-1			
	[-2:+1]	[-3:+2]	[-4:+3]	[-5:+4]			
FIR X Post	0.220***	0.257***	0.271**	* 0.263**			
	(0.056)	(0.074)	(0.087)	(0.098)			
Bond-Month FE	Yes	Yes	Yes	Yes			
Observations	21,106	42,216	63,325	84,433			
N. of Bonds	738	738	738	738			
N. of Countries	68	68	68	68			
N. of Clusters	1,576	1,576	1,576	1,576			
F (FS)	1,667	1,667	1,669	1,670			

Note: This table presents 2SLS estimates of bond log prices on the FIR measure, with each column reporting estimates for different h-day symmetric windows before and after a rebalancing event. The sample period, the construction of h-day windows, and the 2SLS procedure are identical to those described in Table 5. Standard errors are clustered at the country-month level. \*, \*\*\*, and \*\*\* denote statistically significant at the 10%, 5%, and 1% level, respectively.

Appendix Table D6
Log price and FIR: dropping quasi-sovereign bonds

Dependent Variable: Log Price				
FIR	1.078			
	(0.924)			
FIR X Post	0.249**	0.249**	0.249**	0.175*
	(0.107)	(0.108)	(0.107)	(0.103)
Post	0.000	0.000	0.000	
	(0.000)	(0.000)	(0.000)	
Bond FE	Yes	Yes	No	No
Month FE	Yes	No	No	No
Bond Characteristics-Month FE	No	Yes	No	No
Country-Month FE	No	Yes	No	No
Bond-Month FE	No	No	Yes	Yes
Month-Post FE	No	No	No	Yes
Bond Controls	No	Yes	No	No
Observations	73,140	73,100	73,140	73,140
N. of Bonds	430	430	430	430
N. of Countries	65	65	65	65
N. of Clusters	1,513	1,512	1,513	1,513
F (FS)	0	3,151	3,231	1,099

Note: This table presents 2SLS estimates of log bond prices on the FIR measure (Equation (2)), instrumented by Z (Equation (4)), around rebalancing dates. The first- and second-stage equations are described in Equation (5). The estimations use a symmetric five-trading-day window, with Post as an indicator variable (equal to 1 for the five trading days after rebalancing, and 0 otherwise). Month fixed effects are dummy variables equal to 1 for each rebalancing month (0 otherwise), and bond characteristics are fixed effects that interact maturity and ratings fixed effects. Maturity fixed effects are constructed by dividing a bond's time to maturity into four different categories: short (less than 5 years), medium (5-10 years), long (10-20 years), and very long (20+ years). Ratings from each bond are from Moody's. Bond controls indicate whether the estimation includes the log face amount and log stripped spread of the bond. Standard errors are clustered at the country-month level, and the sample period is 2016–2018.  $^{*},$   $^{**},$ and \*\*\* denote statistically significant at the 10%, 5%, and 1% level, respectively.

Appendix Table D7
Log price and FIR: spread heterogeneity (3 groups)

Dependent Variable: Log Price								
	High S	Spread	Median	Spread	Low Spread			
FIR	2.179		0.140		0.391			
	(1.810)		(0.508)		(0.361)			
FIR X Post	0.380**	0.381**	0.325**	0.322**	0.087	0.087		
	(0.166)	(0.165)	(0.152)	(0.151)	(0.098)	(0.098)		
Post	0.001*	0.001*	0.001**	0.001**	-0.000	-0.000		
	(0.001)	(0.001)	(0.000)	(0.000)	(0.000)	(0.000)		
Bond FE	Yes	No	Yes	No	Yes	No		
Month FE	Yes	No	Yes	No	Yes	No		
Bond-Month FE	No	Yes	No	Yes	No	Yes		
Observations	28,105	28,104	28,055	28,053	28,276	28,276		
N. of Bonds	381	381	453	453	375	375		
N. of Countries	58	58	51	51	43	43		
N. of Clusters	975	975	837	837	634	634		
F (FS)	501	2,342	436	720	0	882		

Note: This table presents 2SLS estimates of log bond prices on the FIR measure (Equation (2)), instrumented by Z (Equation (4)), around rebalancing dates. The first- and second-stage equations are described in Equation (5). The estimations use a symmetric four-trading-day window excluding h=-1 and h=+5, with Post as an indicator variable (equal to 1 for the five trading days after rebalancing, and 0 otherwise). The sample is divided into bonds with high spreads (Columns 1 and 2), median spreads (Columns 3 and 4), and low spread (Columns 5 and 6), with spreads divided according to their 33.3 and 66.6 percentile into the three different buckets. Month fixed effects are dummy variables equal to 1 for each rebalancing month, and 0 otherwise. Standard errors are clustered at the country-month level, and the sample period is 2016-2018. \*, \*\*, and \*\*\* denote statistically significant at the 10%, 5%, and 1% level, respectively.